An Insect-Based Algorithm for the Dynamic Task Allocation Problem

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An insect-based algorithm inspired by the division of labor in insect colonies is proposed and applied to the solution of an online scheduling problem. A painting facility is considered for illustrating the problem: Trucks leave an assembly line to get painted in painting booths. The goal is to minimize the makespan, that is, the time needed for painting all given trucks. In this paper we address two issues. First, we propose and analyze four modifications of an insect-based algorithm previously introduced by Cicirello and Smith. Second, we propose an extension of the dynamic threshold model of Theraulaz et al. that was originally used for handling the case in which all booths are identical; in our extension we address the heterogeneous case in which different booths might require different processing times for completing a same task. The paper contains an empirical comparison of different insect-based algorithms for the problem discussed.

1 Introduction

Swarm intelligence techniques [1] have been successfully adopted in computer science, engineering, and operations research. For example, for various combinatorial optimization problems and colony optimization [7] obtains state-of-the-art results.

In this paper we propose an insect-based algorithm for tackling the Dynamic Task Allocation (DTA) problem, a factory scheduling problem in which tasks are to be allocated to processing units. In previous works, multi-agent algorithms have been developed for the homogeneous case, that is, the case in which all agents (processing units) are identical. Here we investigate also the heterogeneous case in which agents can differ in their processing speed. Think for example of a factory with old and new machines or with different sets of machines each optimized for a different class of tasks.

Most of the previously proposed algorithms use paradigms based on the specialization concept: Agents tend to specialize for one type of task in order to avoid unnecessary reconfigurations. This typically increases the efficiency of the whole system. Morley [13] has solved a painting problem similar to the homogeneous version of the DTA problem. His market-based algorithm was adopted in a General Motors facility and reached a performance improvement of 10% over the previously adopted centralized scheduler. Furthermore, different insect-based algorithms have been successfully applied to the homogeneous case of the DTA problem [4, 5]. These algorithms are inspired by the division of labor in social insects and adopt the dynamic threshold model proposed by Theraulaz et al. [15].

In this paper we address two issues. First, we propose four modifications of an algorithm previously introduced by Cicirello and Smith [5]. A detailed analysis of the impact of each modification is given. Second, we propose a modification of the dynamic threshold model of Theraulaz et al. [15] that was originally used for handling the case in which all booths are identical. We present a modified version of the threshold model which takes into account the heterogeneous processing speeds of the agents and we show that the modified version obtains better results than the original version.

Section 2 presents the problem using the example of a painting facility. Section 3 introduces related works, in particular detailing the market-based and two insect-based algorithms. Then, Section 4 explains the algorithm proposed here, showing the modifications we applied to improve the performance. Section 5 proposes an experimental analysis that highlights the performance improvement obtained by the proposed algorithm over the ones previously presented in the literature. Section 6 concludes the paper.

2 The Problem

The problem considered here is a particular nondeterministic scheduling problem that we refer to as the Dynamic Task Allocation (DTA) problem. In the following we describe the problem using the example of a painting facility. A formal definition is given in [9, 8].

Trucks leave an assembly line and are assigned to a painting booth. The number of available colors is fixed and the color of each truck is predetermined by a customer order. A painting booth is an agent able to paint a truck in any available color. Booths may have different processing times for the same type of tasks. Moreover, each booth has a fixed queue length which can be filled with trucks. If the color of a painting booth must be changed, a setup time is necessary. For example, if a booth is applying red and the following truck to be processed by that painting booth requires white, a fixed flush time is needed before the booth can start processing the task. If no setup is necessary, the booth starts immediately to paint the following truck in its queue. A setup may also be related to a monetary cost that could, for example, represent the danger of failure when changing a color, or the amount of paint lost during a swap. The problem consists in assigning trucks to painting booths with the goal of minimizing the makespan, that is, the completion time of the last truck in the system.

In the formalization of the DTA problem, the task generation process is not specified. For example, the release dates and the colors may be distributed exponentially or normally. The distributions may vary dynamically so that at a random
time the probability mix changes and agents need to adapt to the new environment.

### 3 Related Works

In Section 2 we used a painting facility as a real world example of the DTa problem. This example originates from Morley [13], who used a market-based approach for optimizing a scheduler for a GM truck painting facility.

Independently from each other, Campos et al. [4] and Cicirello and Smith [5] used similar insect-based approaches to solve the same problem. They were inspired by a threshold model proposed by Borabeau et al. [1, 2] and Theraulaz et al. [15].

In Section 3.1 we detail Morley's approach to the homogeneous case of the DTa problem in which booths are identical. In Section 3.2 we introduce the threshold model and then explain the two insect-based approaches. Note that all the presented algorithms refer to the homogeneous case of the DTa problem.

#### 3.1 Market Based Approach

Market-based approaches are often used for coordinating asynchronous scheduling operations in the face of imperfect knowledge [6, 12, 10]. The decision process is based on a decentralized bidding mechanism where autonomous agents bid for a task or a resource, which is then assigned to the highest bidder. The agents dynamically adjust their bids according to their capability to solve a task or according to the availability of a resource. In the following we detail the market-based approach to the homogeneous case of the DTa problem. As the original algorithm developed by Morley is a manufacturing application, many details are not available. Therefore, we present here the account of Morley's algorithm that was given by Campos et al. [4].

**Morley [13] (MBA):** Each painting booth autonomously bids for painting a truck. If the queue of a booth is full, the latter does not participate in the bidding process. If we consider a task $j$ of color $c_j$, that is in the storage, a booth $k$ that does not have a full queue participates in the bidding process with a value given by:

$$B_k(j) = \frac{P(1 + Ce(k, j))}{\Delta T_k(j)L}$$  \hspace{1cm} (1)

where $e(k, j)$ is a function that equals 1 if a setup will be required for painting the truck with color $c_j$, and 0 otherwise. $P$, $C$, and $L$ are parameters that weight each component. $\Delta T_k(j)$ is the time until task $j$ starts to be painted in booth $k$, and is determined by the following equation:

$$\Delta T_k(j) = q_{\text{proc}} + n_{\text{setup}} + t_{\text{working}}$$  \hspace{1cm} (2)

where $q$ is the number of trucks in the queue of booth $k$, $q_{\text{proc}}$ is the time required to paint one truck, $n$ is the number of setups required for the trucks in the booth's queue, $t_{\text{setup}}$ is the time required for a setup, and $t_{\text{working}}$ is the time necessary to finish the currently painted truck.

All bids are compared and the respective truck is appended to the queue of the highest bidder. If more than one booth submits the same highest bid, the truck is assigned to the booth that requires no setup to paint it. Otherwise, if all or no booth requires a setup the winner is chosen randomly.

#### 3.2 Insect Based Approach

As shown by Wilson [16] on ant species from the *Pheidole* genus, the concept of division of labor allows the colony to adapt to changing demands. In most species of the investigated genus workers are physically divided into two fractions: The small *minors*, who fulfill most of the quotidian tasks, and the larger *majors*, who are responsible for seed milling, abdominal food storage, defense, or a combination of these. Wilson experimentally changed the proportion of *majors* to *minors*. By reducing the fraction of *minors*, he observed that *majors* get engaged in tasks that are usually performed by *minors*.

Theraulaz et al. have developed a model of response thresholds in order to explain the behaviour observed by Wilson [16]. In this model a set of thresholds is given to each individual performing a task, one threshold for each type of task. A threshold's value represents the level of specialization in that task. Depending on the model, thresholds may remain fixed over time [3], or they may be dynamically updated in respect to the task currently performed [15]. For instance, while an ant is foraging for food, the corresponding threshold would decrease, in this way increasing the level of specialization for that task, whereas the thresholds for all other tasks would increase.

A task emits a stimulus to attract the individuals' attention. Based on this stimulus and on the corresponding threshold, an individual will or will not accept the task. The lower a threshold, the higher the probability to accept a task. Thus a lower threshold represents a higher grade of specialization.

This model is the core of the different insect-based algorithms that will be detailed in the following.

**Campos et al. [4] (ABA):** A painting booth is represented by an agent which autonomously competes to paint a truck. Each agent $k$ has a threshold value $\theta_{k,c_j}$ for each color $c_j$. A stimulus $s_j$ is associated to a truck $j$. The stimulus $s_{c_j}$ is established for each color available in the system and is given by the sum of the stimuli of the unassigned tasks in each particular color.

The probability of booth $k$ to get engaged in task $j$ is given by:

$$P(s_{c_j}, \theta_{k,c_j}) = \frac{s_{c_j}^2}{s_{c_j}^2 + d\theta_{k,c_j}^2 + \Delta T_k(j)}$$  \hspace{1cm} (3)

where $c_j$ is the color of truck $j$ and $\theta_{k,c_j}$ is the threshold of agent $k$ for color $c_j$. $a$ and $b$ are parameters and $\Delta T_k(j)$ is the same time as computed in Equation 2.

Values of $P(s_{c_j}, \theta_{k,c_j})$ are compared and the task is assigned to the booth with the highest value. If the truck $j$ is assigned to booth $k$, the threshold values are updated for all of the booths. $\theta_{k,c_j}$ decreases by the amount $\xi$:

$$\theta_{k,c_j} \rightarrow \theta_{k,c_j} - \xi \hspace{1cm} (4)$$

and the thresholds $\theta_{m,c_j}$ of all other paint booths for color $c_j$ increase by the amount $\phi$:

$$\theta_{m,c_j} \rightarrow \theta_{m,c_j} + \phi \hspace{1cm} \forall m \neq k \hspace{1cm} (5)$$

The parameters $\xi$ and $\phi$ are the learning and forgetting factor, respectively. The thresholds $\theta_{k,c_j}$ are constrained to the interval $[1, 500]$. Equation 4 tries to express the fact that booth
4 Modifications to the Insect-Based Approach

In this section we introduce an original insect-based algorithm for the DTA problem. In Section 4.1 we propose four modifications to R-WASP, with the goal to improve its performance [14]. We name the proposed algorithm Ant-Task-Allocation (ATA). In Section 4.2 a modification is introduced that takes into account the different process times for the heterogeneous case of the DTA problem. This modification can be applied to all the insect-based algorithms.

4.1 General Modifications: ATA

Threshold Update Rules (TUR): The update rules proposed by Cicirello and Smith are based on the type of task that is currently processed. The threshold of the currently processed task is reduced, all other thresholds are increased. This is motivated by the behaviour on social insects, who specialize in the task they are performing and tend to continue the task rather than switching it, in this way avoiding the cost in time that would be related to such a switch. However, for the DTA problem the situation is not the same. As each painting booth has a queue that can be filled with tasks, whether a given task causes a setup depends on the type of the last task in the agent's queue, not on the one currently processed. Therefore, in ATA it is the last job in a machine's queue that determines how the threshold values are updated.

**Calculation of the Force Variable (CFV):** The force variable used for the dominance contest does not take into account whether a setup would be required for the respective task. Therefore, in ATA the force value becomes

\[
P_h(F_1, \ldots, F_n) = \frac{1}{F_h^2 + \sum_{i=1}^{n} F_i^2},
\]

(10)

where \(t_{\text{setup}}^i\) is 0 in case no setup is necessary, and the required setup time otherwise.

**Dominance Contest (DC):** Another problem of the dominance contest is that the machines compete with each other in a dominance contest, the smaller are the differences between the probabilities to win. In general the probability for one competitor to win a dominance contest with \(n\) competitors is never higher than \(\frac{1}{n+1}\). In ATA this problem is overcome by using the following rule instead of the one specified in Equation 9:

\[
P_h(F_1, \ldots, F_n) = \frac{1}{\sum_{i \neq h} F_i^2},
\]

(11)

**Idle Machine does not Compete (IMC):** Equation 7 is applied for idle agents in order to encourage the agent to compete for tasks of any type. In ATA an additional rule is introduced aiming specifically at idle agents which ignore tasks that are currently in the system and not allocated yet. In case an idle agent refuses to bid for such a task, the threshold for the respective color is diminished:

\[
\theta_{h,c_j} \rightarrow \theta_{h,c_j} - \gamma.
\]

(12)

4.2 Modification for the Heterogeneous Case

The definition of the DTA problem considers agents that can have different processing times for different task types. The presented algorithms can in principle be applied to the DTA problem. Nevertheless, they do not take into account the different processing speeds of the agents, and therefore their performance is rather poor, as it is shown in Section 5.2. The problem is that agents compete for a task considering only their specialization level without taking into account their own characteristics, that is, their speed in processing a task. In order to overcome this, we extend the threshold model so that the faster an agent can perform a task, the higher is the probability that the agent competes for it. To this aim we introduced the processing speed of agent \(k\) on task \(j\) into the probability function \(P(s_j, \theta_{k,c_j})\) by substituting the threshold \(\theta_{k,c_j}\) in Equations 3 and 6 with \(\theta_{k,c_j}^2\):

\[
\theta_{k,c_j}^2 = \theta_{k,c_j}^2 (t_{\text{proc}}^j - t_{\text{min,proc}}^j + 1),
\]

(13)
where \( t_{\text{proc}}^{k,j} \) is the time that agent \( k \) requires to process task \( j \) and \( t_{\text{min}}^{j} \) is the minimum time needed by agents in the system for processing task \( j \). The additional term serves as a weighting factor of the specialization level. We have tested several different substitutions of the threshold value in the probability functions, with the one given by Equation 13 yielding the best results. The substitution described in Equation 13 can be used for the three insect-based algorithms described above. In the following we call ABAC, R-WASP, and ATAC, the modifications of ABA, R-WASP, and ATA, respectively.

## 5 Empirical Analysis

We have conducted two series of experiments in order to analyze (i) the impact of the modifications we have applied to R-WASP, (ii) the impact of Equation 13 when applied to the heterogeneous DTA problem. All parameters were tuned separately for each approach using an evolutionary algorithm. All algorithms were devoted the same tuning effort. Table 1 summarizes the tuned parameters. For more details we refer to [9, 8].

<table>
<thead>
<tr>
<th>Algorithm</th>
<th>Tuned Parameters</th>
</tr>
</thead>
<tbody>
<tr>
<td>MBA</td>
<td>( P, C, L )</td>
</tr>
<tr>
<td>ABA, ABAC</td>
<td>( \alpha, \beta, \xi, \phi )</td>
</tr>
<tr>
<td>R-WASP, R-WASPc</td>
<td>( \delta, \xi, \phi )</td>
</tr>
<tr>
<td>ATAC</td>
<td>( \delta, \xi, \phi, \gamma )</td>
</tr>
</tbody>
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Table 1: Summary of the tuned parameters.

### 5.1 General Modifications: ATAC

In this section we compare all possible modifications proposed with the ATAC algorithm on a class of instances of the homogeneous case of the DTA problem. In the following we present the experimental setup, the analyzed algorithms and the results.

**Experimental Setup:** The instances in our experimental analysis model a typical working day of a painting facility. Trucks exit from the assembly line for a time of 420 minutes. We consider 24 painting booths. Each painting booth might be broken or anyway unavailable with a probability of 0.02. Each agent has a queue size equal to 5. As we focus on the analysis of the four modifications, we apply the algorithms to the homogeneous case of the DTA problem. All booths require 5 minutes to paint a truck and an additional 10 minutes in case a setup is necessary.

The number of trucks exiting the assembly line is always equal to 2016, which is the maximum number of trucks that 24 booths can paint considering a process time of 5 minutes when no setups are required\(^1\).

For each instance, the number of different colors is chosen with respect to the distribution shown in Figure 1. Color types are assigned to the trucks according to the two probability mixes:

1. Two subsets of the \( n \) colors are considered. Colors in the first subset have a higher probability of being selected than those in the second subset. The probability \( P(c) \) of selecting color \( c \) is defined as follows:

\[
P(c) = \begin{cases} 
\frac{1}{2^{n/2}} & \text{if } c \leq \lfloor n/2 \rfloor \\
\frac{3}{2^{n/2}} & \text{if } c > \lfloor n/2 \rfloor 
\end{cases}
\]

2. Like the previous one, but after 210 minutes the colors that appear more frequently appear more rarely and vice versa. Each instance features either one mix or the other, with the same probability.

**Algorithms:** As there are four proposed modifications there are 16 possible combinations of the proposed modifications which are all analyzed. We use a binary notation with four bits to identify these combinations. The first bit represents whether or not TUR is active, the second bit represents CFV, the third DC, and the last IMC. For instance, 0000 indicates that no rules are active, 1000 means that only TUR is active, and so on.

**Results:** We have run all the algorithms on 1,000 instances of the considered problem class. Figure 2 summarizes the results, which show that, on average, configuration 1011 performs best, and that ATAC (configuration 1111) is very close to it. Moreover, all possible configurations have a lower makespan than R-WASP (configuration 0000), indicating that each modification has a positive impact on the performance. Furthermore, the rule with the highest impact on the performance is TUR: indeed the configurations on the right-hand side of Figure 2, in which TUR is active, are apparently better than those on the left-hand side.

### 5.2 Modification for the Heterogeneous Case

In this section we compare the presented algorithms on a class of instances of the heterogeneous DTA problem. In the following we present the experimental setup, all the analyzed algorithms and the results.

**Experimental Setup:** The setup used is very similar to the previous one. The differences are that instead of 24 we consider 12 painting booths, and that we extract the number of colors from the probability distribution presented in Figure 3. Furthermore, given that we analyze the heterogeneous case of the DTA, there are two subsets of agents: the first needs 3 minutes to process the first half of the available types of tasks and 9 minutes for the other half. The other

\(^1\) 24 booths * 420 time steps / 5 time steps per truck = 2016.
Figure 2: Box plot of the makespan values for all 16 possible combinations of the four modifications to R-WASP when applied to the homogeneous DTA problem. Binary numbers indicate usage of the modifications TUR, CFV, DC, and IMC.

Figure 3: Probability distribution of the number of colors for the DTA experiment.

subset has the opposite characteristics, that is, 5 and 3 minutes are respectively needed for the two subsets. For both subsets the setup time is 10 minutes.

Algorithms: In this analysis we compare the four previously described algorithms MBA, ABA, R-WASP and ATA. To evaluate the performance of the modified threshold value (see Equation 13), we have applied it to all insect-based algorithms, which are named ABAC, R-WASPc, ATAc. Additionally, a trivial non-adaptive greedy algorithm named LOCUST is introduced in order to have a performance reference. Applying LOCUST, trucks are allocated to booths following the dominance contest as used by R-WASP.

Results: We have run all the algorithms on 1,000 instances of the considered class.

Figure 4 summarizes the results for the DTA experiment. The values and ranks are shown in Figure 4(a) and (b) for the makespan, and in Figure 4(c) and (d) for the number of setups. Among the eight compared algorithms, ATAc obtains the best results. It achieves makespan values which are very close to the lower bound of 420 minutes. Furthermore, it reaches on average the lowest number of required setups. On the basis of a paired Wilcoxon test ($\alpha = .05$) we can state that: i) the adaptive algorithms perform significantly better than the non-adaptive algorithm LOCUST. ii) The algorithms that use the modified calculation of the threshold value (see Equation 13) significantly better than the respective algorithms that use the original one.

Interestingly, ATA achieves a low makespan and requires a low number of setups. It is the only algorithm that achieves this without the modification proposed in Section 4.2. This suggests that the four proposed modifications with respect to R-WASP are robust enough to cope with the heterogeneous case of the DTA problem. While R-WASPc is the algorithm that benefits the most from the modification, the improvement is smaller for ABA.

6 Conclusion

In this paper we have presented an insect-based algorithm for the solution of a scheduling problem in which tasks have to be assigned to processing units. The algorithm is an extension of a previously presented algorithm by Cicirello and Smith [5] based on the dynamic threshold model. We showed that each modification proposed leads to a better performance. In particular, the modification of the threshold update rules, TUR (see Section 4.1 for details), is the modification with the highest impact.

Furthermore, we addressed the heterogeneous case of the DTA problem in which different groups of booths require different processing times for completing a same task. We introduced a simple modification to the insect-based algorithms that significantly improves their performances. The modification, given by Equation 13, consists in a substitution of the threshold value in the probability functions, in this way taking into account the different processing times of the painting booths.

A number of issues deserve further analysis. For instance, the substitution of the threshold value we have chosen is just one out of many that would be possible. Even though we have achieved promising results, a problem of the current implementation is that rescaling processing times would lead to a different outcome in the respective probability function. A different parameter set would therefore be required. One possible solution to this problem could be to divide rather than to subtract the two terms $t_{j}^{\text{proc}}$ and $t_{j}^{\text{min.proc}}$ in Equation 13.

Furthermore, an analysis of the parameter space for each analyzed algorithm might be worthwhile. Kittithreeraprontchai and Anderson [11] have already addressed this topic for ABA and MBA. They found that the parameter surfaces are surprisingly smooth, and were able to identify key parameters.

Acknowledgements. This research has been supported by ANTS, an Action de Recherche Concertée funded by the French Community of Belgium. Marco Dorigo acknowledges support from the Belgian FNRS, of which he is a Research Director. The authors thank the reviewers for their helpful suggestions and comments.
Figure 4: Results for the DTA experiment, showing box plots of (a) the makespan values, (b) the makespan ranks, (c) the values for the number of setups, and (d) the ranks for the number of setups for the eight algorithms. The figure shows that the improved model leads to an improvement of the performance especially to the R-WASP algorithm.

References


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