

Complete Numerical Results for the Paper  
Estimation-based Ant Colony Optimization  
and Local Search for the  
Probabilistic Traveling Salesman Problem

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# 1 Effectiveness of 2.5-opt-EEais in pACS

Table 1: Comparison of the average cost obtained by pACS+2.5-opt-EEais and pACS+1-shift over 30 independent runs on the PTSPLIB instance rat783. The table gives, for each probability level, the mean and the standard deviation (s.d.) of the final solution cost over 30 instances.

	Algorithm	Solution Cost	
		mean	s.d.
$p = 0.050$	pACS+2.5-opt-EEais	2319	3
	pACS+1-shift	2314	14
$p = 0.075$	pACS+2.5-opt-EEais	2817	3
	pACS+1-shift	2875	37
$p = 0.100$	pACS+2.5-opt-EEais	3245	3
	pACS+1-shift	3346	36
$p = 0.150$	pACS+2.5-opt-EEais	3956	8
	pACS+1-shift	4173	65
$p = 0.175$	pACS+2.5-opt-EEais	4268	9
	pACS+1-shift	4530	56
$p = 0.200$	pACS+2.5-opt-EEais	4548	9
	pACS+1-shift	4850	57
$p = 0.300$	pACS+2.5-opt-EEais	5490	12
	pACS+1-shift	6060	86
$p = 0.400$	pACS+2.5-opt-EEais	6230	15
	pACS+1-shift	6981	131
$p = 0.500$	pACS+2.5-opt-EEais	6851	10
	pACS+1-shift	7800	123

Table 2: Comparison of the average cost obtained by pACS+2.5-opt-EEais and pACS+1-shift over 30 independent runs on the PTSPLIB instance att532. The table gives, for each probability level, the mean and the standard deviation (s.d.) of the final solution cost over 30 instances.

	Algorithm	Solution Cost	
		mean	s.d.
$p = 0.050$	pACS+2.5-opt-EEais	25511	2
	pACS+1-shift	25484	3
$p = 0.075$	pACS+2.5-opt-EEais	29952	4
	pACS+1-shift	29976	88
$p = 0.100$	pACS+2.5-opt-EEais	33702	12
	pACS+1-shift	33893	188
$p = 0.150$	pACS+2.5-opt-EEais	39700	44
	pACS+1-shift	40453	300
$p = 0.175$	pACS+2.5-opt-EEais	42272	26
	pACS+1-shift	43299	396
$p = 0.200$	pACS+2.5-opt-EEais	44692	22
	pACS+1-shift	45936	451
$p = 0.300$	pACS+2.5-opt-EEais	53101	83
	pACS+1-shift	55854	640
$p = 0.400$	pACS+2.5-opt-EEais	59967	99
	pACS+1-shift	64365	910
$p = 0.500$	pACS+2.5-opt-EEais	66053	95
	pACS+1-shift	72528	1223

Table 3: Comparison of the average cost obtained by pACS+2.5-opt-EEais and pACS+1-shift over 30 independent runs on the PTSPLIB instance lin318. The table gives, for each probability level, the mean and the standard deviation (s.d.) of the final solution cost over 30 instances.

	Algorithm	Solution Cost	
		mean	s.d.
$p = 0.050$	pACS+2.5-opt-EEais	12580	2
	pACS+1-shift	12558	0
$p = 0.075$	pACS+2.5-opt-EEais	15084	3
	pACS+1-shift	15068	0
$p = 0.100$	pACS+2.5-opt-EEais	17205	2
	pACS+1-shift	17194	3
$p = 0.150$	pACS+2.5-opt-EEais	20690	4
	pACS+1-shift	20742	97
$p = 0.175$	pACS+2.5-opt-EEais	22160	7
	pACS+1-shift	22412	183
$p = 0.200$	pACS+2.5-opt-EEais	23500	76
	pACS+1-shift	23846	155
$p = 0.300$	pACS+2.5-opt-EEais	27879	149
	pACS+1-shift	28821	408
$p = 0.400$	pACS+2.5-opt-EEais	31222	110
	pACS+1-shift	32506	478
$p = 0.500$	pACS+2.5-opt-EEais	33851	93
	pACS+1-shift	35843	452

Table 4: Comparison of the average cost obtained by pACS+2.5-opt-EEais and pACS+1-shift over 30 independent runs on the PTSPLIB instance d198. The table gives, for each probability level, the mean and the standard deviation (s.d.) of the final solution cost over 30 instances.

	Algorithm	Solution Cost	
		mean	s.d.
$p = 0.050$	pACS+2.5-opt-EEais	5609	0
	pACS+1-shift	5606	0
$p = 0.075$	pACS+2.5-opt-EEais	6672	0
	pACS+1-shift	6670	0
$p = 0.100$	pACS+2.5-opt-EEais	7439	1
	pACS+1-shift	7437	0
$p = 0.150$	pACS+2.5-opt-EEais	8527	1
	pACS+1-shift	8524	0
$p = 0.175$	pACS+2.5-opt-EEais	8944	1
	pACS+1-shift	8940	0
$p = 0.200$	pACS+2.5-opt-EEais	9316	1
	pACS+1-shift	9312	0
$p = 0.300$	pACS+2.5-opt-EEais	10537	5
	pACS+1-shift	10536	12
$p = 0.400$	pACS+2.5-opt-EEais	11536	3
	pACS+1-shift	11565	36
$p = 0.500$	pACS+2.5-opt-EEais	12420	4
	pACS+1-shift	12486	50

Table 5: Comparison of the average cost obtained by pACS+2.5-opt-EEais and pACS+1-shift over 30 independent runs on the PTSPLIB instance ch150. The table gives, for each probability level, the mean and the standard deviation (s.d.) of the final solution cost over 30 instances.

	Algorithm	Solution Cost	
		mean	s.d.
$p = 0.050$	pACS+2.5-opt-EEais	1771	1
	pACS+1-shift	1767	0
$p = 0.075$	pACS+2.5-opt-EEais	2164	1
	pACS+1-shift	2161	0
$p = 0.100$	pACS+2.5-opt-EEais	2481	0
	pACS+1-shift	2479	0
$p = 0.150$	pACS+2.5-opt-EEais	3012	1
	pACS+1-shift	3010	0
$p = 0.175$	pACS+2.5-opt-EEais	3235	4
	pACS+1-shift	3232	2
$p = 0.200$	pACS+2.5-opt-EEais	3421	6
	pACS+1-shift	3417	0
$p = 0.300$	pACS+2.5-opt-EEais	4055	5
	pACS+1-shift	4054	5
$p = 0.400$	pACS+2.5-opt-EEais	4574	7
	pACS+1-shift	4580	10
$p = 0.500$	pACS+2.5-opt-EEais	5005	4
	pACS+1-shift	5028	24

Table 6: Comparison of the average cost obtained by pACS+2.5-opt-EEais and pACS+1-shift over 30 independent runs on the PTSPLIB instance eil101. The table gives, for each probability level, the mean and the standard deviation (s.d.) of the final solution cost over 30 instances.

	Algorithm	Solution Cost	
		mean	s.d.
$p = 0.050$	pACS+2.5-opt-EEais	133	0
	pACS+1-shift	132	0
$p = 0.075$	pACS+2.5-opt-EEais	170	0
	pACS+1-shift	169	0
$p = 0.100$	pACS+2.5-opt-EEais	197	0
	pACS+1-shift	196	0
$p = 0.150$	pACS+2.5-opt-EEais	243	0
	pACS+1-shift	242	0
$p = 0.175$	pACS+2.5-opt-EEais	264	0
	pACS+1-shift	263	0
$p = 0.200$	pACS+2.5-opt-EEais	283	0
	pACS+1-shift	282	0
$p = 0.300$	pACS+2.5-opt-EEais	348	1
	pACS+1-shift	346	0
$p = 0.400$	pACS+2.5-opt-EEais	402	1
	pACS+1-shift	401	0
$p = 0.500$	pACS+2.5-opt-EEais	450	0
	pACS+1-shift	450	1

Table 7: Comparison of the average cost obtained by pACS+2.5-opt-EEais and pACS+1-shift over 30 independent runs on the PTSP LIB instance kroA100. The table gives, for each probability level, the mean and the standard deviation (s.d.) of the final solution cost over 30 instances.

	Algorithm	Solution Cost	
		mean	s.d.
$p = 0.050$	pACS+2.5-opt-EEais	6470	1
	pACS+1-shift	6465	0
$p = 0.075$	pACS+2.5-opt-EEais	8021	1
	pACS+1-shift	8016	0
$p = 0.100$	pACS+2.5-opt-EEais	9038	1
	pACS+1-shift	9034	0
$p = 0.150$	pACS+2.5-opt-EEais	10521	0
	pACS+1-shift	10520	0
$p = 0.175$	pACS+2.5-opt-EEais	11142	0
	pACS+1-shift	11142	0
$p = 0.200$	pACS+2.5-opt-EEais	11715	1
	pACS+1-shift	11714	0
$p = 0.300$	pACS+2.5-opt-EEais	13680	1
	pACS+1-shift	13678	0
$p = 0.400$	pACS+2.5-opt-EEais	15253	0
	pACS+1-shift	15253	0
$p = 0.500$	pACS+2.5-opt-EEais	16569	0
	pACS+1-shift	16569	0

Table 8: Comparison of the average cost obtained by `pACS+2.5-opt-EEais` and `pACS+1-shift` over 30 independent runs on the PTSPLIB instance rat783. The table reports the observed relative difference and a 95% confidence interval (CI) obtained through the t-test on the relative difference. For a given comparison  $A$  vs.  $B$ , the table reports the observed relative difference between the two algorithms  $A$  and  $B$  and a 95% confidence interval (CI) obtained through the t-test. If the value is positive, algorithm  $A$  obtained an average cost that is larger than the one obtained by the algorithm  $B$ . In this case, the value is typeset in italics if it is significantly different from zero according to the t-test at a confidence of 95%. If the value is negative, algorithm  $A$  obtained an average cost that is smaller than the one obtained by the algorithm  $B$ . In this case, the value is typeset in boldface if it is significantly different from zero according to the t-test, at a confidence of 95%.

$p$	pACS+2.5-opt-EEais vs. pACS+1-shift	
	Difference	95% CI
0.050-00	<i>+0.236</i>	[+0.014, +0.459]
0.075-00	<b>-2.022</b>	[-2.509, -1.534]
0.100-00	<b>-3.029</b>	[-3.430, -2.628]
0.150-00	<b>-5.214</b>	[-5.784, -4.644]
0.175-00	<b>-5.798</b>	[-6.270, -5.326]
0.200-00	<b>-6.214</b>	[-6.661, -5.766]
0.300-00	<b>-9.401</b>	[-9.924, -8.877]
0.400-00	<b>-10.760</b>	[-11.451, -10.069]
0.500-00	<b>-12.176</b>	[-12.759, -11.593]

Table 9: Comparison of the average cost obtained by **pACS+2.5-opt-EEais** and **pACS+1-shift** over 30 independent runs on the PTSPLIB instance att532. The table reports the observed relative difference and a 95% confidence interval (CI) obtained through the t-test on the relative difference. For a given comparison  $A$  vs.  $B$ , the table reports the observed relative difference between the two algorithms  $A$  and  $B$  and a 95% confidence interval (CI) obtained through the t-test. If the value is positive, algorithm  $A$  obtained an average cost that is larger than the one obtained by the algorithm  $B$ . In this case, the value is typeset in italics if it is significantly different from zero according to the t-test at a confidence of 95%. If the value is negative, algorithm  $A$  obtained an average cost that is smaller than the one obtained by the algorithm  $B$ . In this case, the value is typeset in boldface if it is significantly different from zero according to the t-test, at a confidence of 95%.

$p$	pACS+2.5-opt-EEais vs. pACS+1-shift	
	Difference	95% CI
0.050-00	+ <i>0.105</i>	[+0.099, +0.110]
0.075-00	-0.080	[-0.190, +0.031]
0.100-00	<b>-0.564</b>	[-0.771, -0.357]
0.150-00	<b>-1.862</b>	[-2.153, -1.571]
0.175-00	<b>-2.374</b>	[-2.716, -2.031]
0.200-00	<b>-2.708</b>	[-3.072, -2.345]
0.300-00	<b>-4.930</b>	[-5.375, -4.485]
0.400-00	<b>-6.834</b>	[-7.369, -6.298]
0.500-00	<b>-8.928</b>	[-9.550, -8.306]

Table 10: Comparison of the average cost obtained by pACS+2.5-opt-EEais and pACS+1-shift over 30 independent runs on the PTSPLIB instance lin318. The table reports the observed relative difference and a 95% confidence interval (CI) obtained through the t-test on the relative difference. For a given comparison  $A$  vs.  $B$ , the table reports the observed relative difference between the two algorithms  $A$  and  $B$  and a 95% confidence interval (CI) obtained through the t-test. If the value is positive, algorithm  $A$  obtained an average cost that is larger than the one obtained by the algorithm  $B$ . In this case, the value is typeset in italics if it is significantly different from zero according to the t-test at a confidence of 95%. If the value is negative, algorithm  $A$  obtained an average cost that is smaller than the one obtained by the algorithm  $B$ . In this case, the value is typeset in boldface if it is significantly different from zero according to the t-test, at a confidence of 95%.

<i>p</i>	pACS+2.5-opt-EEais vs. pACS+1-shift	
	Difference	95% CI
0.100-00	+0.066	[+0.058, +0.074]
0.150-00	<b>-0.251</b>	[-0.427, -0.075]
0.175-00	<b>-1.122</b>	[-1.428, -0.815]
0.200-00	<b>-1.451</b>	[-1.732, -1.170]
0.300-00	<b>-3.269</b>	[-3.803, -2.735]
0.400-00	<b>-3.950</b>	[-4.517, -3.383]
0.500-00	<b>-5.558</b>	[-6.014, -5.102]

Table 11: Comparison of the average cost obtained by **pACS+2.5-opt-EEais** and **pACS+1-shift** over 30 independent runs on the PTSPLIB instance d198. The table reports the observed relative difference and a 95% confidence interval (CI) obtained through the t-test on the relative difference. For a given comparison  $A$  vs.  $B$ , the table reports the observed relative difference between the two algorithms  $A$  and  $B$  and a 95% confidence interval (CI) obtained through the t-test. If the value is positive, algorithm  $A$  obtained an average cost that is larger than the one obtained by the algorithm  $B$ . In this case, the value is typeset in italics if it is significantly different from zero according to the t-test at a confidence of 95%. If the value is negative, algorithm  $A$  obtained an average cost that is smaller than the one obtained by the algorithm  $B$ . In this case, the value is typeset in boldface if it is significantly different from zero according to the t-test, at a confidence of 95%.

<i>p</i>	pACS+2.5-opt-EEais vs. pACS+1-shift	
	Difference	95% CI
0.300-00	+0.009	[−0.035, +0.054]
0.400-00	<b>−0.250</b>	[−0.366, −0.134]
0.500-00	<b>−0.534</b>	[−0.684, −0.385]

Table 12: Comparison of the average cost obtained by `pACS+2.5-opt-EEais` and `pACS+1-shift` over 30 independent runs on the PTSPLIB instance ch150. The table reports the observed relative difference and a 95% confidence interval (CI) obtained through the t-test on the relative difference. For a given comparison  $A$  vs.  $B$ , the table reports the observed relative difference between the two algorithms  $A$  and  $B$  and a 95% confidence interval (CI) obtained through the t-test. If the value is positive, algorithm  $A$  obtained an average cost that is larger than the one obtained by the algorithm  $B$ . In this case, the value is typeset in italics if it is significantly different from zero according to the t-test at a confidence of 95%. If the value is negative, algorithm  $A$  obtained an average cost that is smaller than the one obtained by the algorithm  $B$ . In this case, the value is typeset in boldface if it is significantly different from zero according to the t-test, at a confidence of 95%.

$p$	pACS+2.5-opt-EEais vs. pACS+1-shift	
	Difference	95% CI
0.175-00	<i>+0.093</i>	[+0.042, +0.144]
0.300-00	+0.042	[-0.009, +0.093]
0.400-00	<b>-0.118</b>	[-0.217, -0.019]
0.500-00	<b>-0.459</b>	[-0.647, -0.272]

Table 13: Comparison of the average cost obtained by **pACS+2.5-opt-EEais** and **pACS+1-shift** over 30 independent runs on the PTSPLIB instance eil101. The table reports the observed relative difference and a 95% confidence interval (CI) obtained through the t-test on the relative difference. For a given comparison  $A$  vs.  $B$ , the table reports the observed relative difference between the two algorithms  $A$  and  $B$  and a 95% confidence interval (CI) obtained through the t-test. If the value is positive, algorithm  $A$  obtained an average cost that is larger than the one obtained by the algorithm  $B$ . In this case, the value is typeset in italics if it is significantly different from zero according to the t-test at a confidence of 95%. If the value is negative, algorithm  $A$  obtained an average cost that is smaller than the one obtained by the algorithm  $B$ . In this case, the value is typeset in boldface if it is significantly different from zero according to the t-test, at a confidence of 95%.

<i>p</i>	pACS+2.5-opt-EEais vs. pACS+1-shift	
	Difference	95% CI
0.400-00	+0.116	[+0.008, +0.225]
0.500-00	-0.007	[-0.063, +0.048]

## 2 Estimation-based ant colony system

Table 14: Comparison of the average cost obtained by ACS-EE and pACS+2.5-opt-EEais on instance ch150 for  $n^2/10000$  CPU seconds

	Algorithm	Solution Cost	
		mean	s.d.
$p = 0.050$	ACS-EE	1775	2
	pACS	1775	3
$p = 0.075$	ACS-EE	2166	1
	pACS	2166	1
$p = 0.100$	ACS-EE	2486	4
	pACS	2483	1
$p = 0.150$	ACS-EE	3016	2
	pACS	3015	5
$p = 0.175$	ACS-EE	3242	4
	pACS	3236	4
$p = 0.200$	ACS-EE	3421	1
	pACS	3425	8
$p = 0.300$	ACS-EE	4060	8
	pACS	4062	9
$p = 0.400$	ACS-EE	4582	9
	pACS	4580	10
$p = 0.500$	ACS-EE	5012	13
	pACS	5013	11

Table 15: Comparison of the average cost obtained by ACS-EE and pACS+2.5-opt-EEais on instance ch150 for  $n^2/1000$  CPU seconds

	Algorithm	Solution Cost	
		mean	s.d.
$p = 0.050$	ACS-EE	1774	1
	pACS	1773	2
$p = 0.075$	ACS-EE	2166	1
	pACS	2165	1
$p = 0.100$	ACS-EE	2485	2
	pACS	2482	0
$p = 0.150$	ACS-EE	3015	1
	pACS	3015	6
$p = 0.175$	ACS-EE	3242	3
	pACS	3237	5
$p = 0.200$	ACS-EE	3420	0
	pACS	3424	7
$p = 0.300$	ACS-EE	4060	7
	pACS	4059	8
$p = 0.400$	ACS-EE	4576	8
	pACS	4576	7
$p = 0.500$	ACS-EE	5010	6
	pACS	5010	9

Table 16: Comparison of the average cost obtained by ACS-EE and pACS+2.5-opt-EEais on instance d198 for for  $n^2/10000$  CPU seconds.

	Algorithm	Solution Cost	
		mean	s.d.
$p = 0.050$	ACS-EE	5638	36
	pACS	5625	19
$p = 0.075$	ACS-EE	6682	6
	pACS	6680	5
$p = 0.100$	ACS-EE	7446	3
	pACS	7443	3
$p = 0.150$	ACS-EE	8534	4
	pACS	8532	4
$p = 0.175$	ACS-EE	8949	3
	pACS	8947	2
$p = 0.200$	ACS-EE	9324	3
	pACS	9321	4
$p = 0.300$	ACS-EE	10550	5
	pACS	10547	5
$p = 0.400$	ACS-EE	11546	3
	pACS	11547	10
$p = 0.500$	ACS-EE	12427	4
	pACS	12427	11

Table 17: Comparison of the average cost obtained by ACS-EE and pACS+2.5-opt-EEais on instance d198 for for  $n^2/1000$  CPU seconds.

	Algorithm	Solution Cost	
		mean	s.d.
$p = 0.050$	ACS-EE	5613	2
	pACS	5613	2
$p = 0.075$	ACS-EE	6677	2
	pACS	6674	1
$p = 0.100$	ACS-EE	7446	3
	pACS	7440	1
$p = 0.150$	ACS-EE	8533	2
	pACS	8528	1
$p = 0.175$	ACS-EE	8948	2
	pACS	8945	1
$p = 0.200$	ACS-EE	9324	2
	pACS	9318	1
$p = 0.300$	ACS-EE	10544	4
	pACS	10542	5
$p = 0.400$	ACS-EE	11543	4
	pACS	11540	4
$p = 0.500$	ACS-EE	12424	6
	pACS	12422	4

Table 18: Comparison of the average cost obtained by ACS-EE and pACS+2.5-opt-EEais on instance lin318 for  $n^2/10000$  CPU seconds.

	Algorithm	Solution Cost	
		mean	s.d.
$p = 0.050$	ACS-EE	12720	80
	pACS	12734	89
$p = 0.075$	ACS-EE	15174	55
	pACS	15174	67
$p = 0.100$	ACS-EE	17408	74
	pACS	17378	89
$p = 0.150$	ACS-EE	20960	128
	pACS	20875	88
$p = 0.175$	ACS-EE	22455	136
	pACS	22432	103
$p = 0.200$	ACS-EE	23727	146
	pACS	23846	172
$p = 0.300$	ACS-EE	28193	156
	pACS	28170	160
$p = 0.400$	ACS-EE	31414	158
	pACS	31479	177
$p = 0.500$	ACS-EE	34041	124
	pACS	34127	176

Table 19: Comparison of the average cost obtained by ACS-EE and pACS+2.5-opt-EEais on instance lin318 for  $n^2/1000$  CPU seconds.

	Algorithm	Solution Cost	
		mean	s.d.
$p = 0.050$	ACS-EE	12596	8
	pACS	12593	8
$p = 0.075$	ACS-EE	15107	8
	pACS	15094	4
$p = 0.100$	ACS-EE	17223	8
	pACS	17212	5
$p = 0.150$	ACS-EE	20762	62
	pACS	20719	37
$p = 0.175$	ACS-EE	22246	72
	pACS	22208	56
$p = 0.200$	ACS-EE	23522	59
	pACS	23533	75
$p = 0.300$	ACS-EE	28011	125
	pACS	27990	165
$p = 0.400$	ACS-EE	31266	92
	pACS	31319	143
$p = 0.500$	ACS-EE	33900	97
	pACS	33923	105

Table 20: Comparison of the average cost obtained by ACS-EE and pACS+2.5-opt-EEais on instance att532 for  $n^2/10000$  CPU seconds.

	Algorithm	Solution Cost	
		mean	s.d.
$p = 0.050$	ACS-EE	25844	186
	pACS	25821	176
$p = 0.075$	ACS-EE	30248	192
	pACS	30161	124
$p = 0.100$	ACS-EE	33890	92
	pACS	33864	75
$p = 0.150$	ACS-EE	40051	108
	pACS	40082	155
$p = 0.175$	ACS-EE	42724	201
	pACS	42723	184
$p = 0.200$	ACS-EE	45363	203
	pACS	45193	171
$p = 0.300$	ACS-EE	53884	309
	pACS	53775	228
$p = 0.400$	ACS-EE	60710	185
	pACS	60761	264
$p = 0.500$	ACS-EE	66690	230
	pACS	66752	263

Table 21: Comparison of the average cost obtained by ACS-EE and pACS+2.5-opt-EEais on instance att532 for  $n^2/1000$  CPU seconds.

	Algorithm	Solution Cost	
		mean	s.d.
$p = 0.050$	ACS-EE	25534	13
	pACS	25532	12
$p = 0.075$	ACS-EE	29992	11
	pACS	29981	11
$p = 0.100$	ACS-EE	33734	23
	pACS	33730	18
$p = 0.150$	ACS-EE	39779	39
	pACS	39750	42
$p = 0.175$	ACS-EE	42373	88
	pACS	42347	87
$p = 0.200$	ACS-EE	44775	88
	pACS	44755	51
$p = 0.300$	ACS-EE	53271	176
	pACS	53185	99
$p = 0.400$	ACS-EE	60177	180
	pACS	60196	141
$p = 0.500$	ACS-EE	66201	115
	pACS	66192	134

Table 22: Comparison of the average cost obtained by ACS-EE and pACS+2.5-opt-EEais on instance rat783 for  $n^2/10000$  CPU seconds.

	Algorithm	Solution Cost	
		mean	s.d.
$p = 0.050$	ACS-EE	2360	13
	pACS	2358	14
$p = 0.075$	ACS-EE	2856	12
	pACS	2859	10
$p = 0.100$	ACS-EE	3290	12
	pACS	3293	13
$p = 0.150$	ACS-EE	4018	17
	pACS	4021	9
$p = 0.175$	ACS-EE	4338	16
	pACS	4339	14
$p = 0.200$	ACS-EE	4634	16
	pACS	4634	23
$p = 0.300$	ACS-EE	5617	20
	pACS	5621	21
$p = 0.400$	ACS-EE	6356	27
	pACS	6363	21
$p = 0.500$	ACS-EE	6969	21
	pACS	6977	21

Table 23: Comparison of the average cost obtained by ACS-EE and pACS+2.5-opt-EEais on instance rat783 for  $n^2/1000$  CPU seconds.

	Algorithm	Solution Cost	
		mean	s.d.
$p = 0.050$	ACS-EE	2329	4
	pACS	2328	4
$p = 0.075$	ACS-EE	2832	6
	pACS	2830	4
$p = 0.100$	ACS-EE	3260	6
	pACS	3258	5
$p = 0.150$	ACS-EE	3970	8
	pACS	3969	7
$p = 0.175$	ACS-EE	4281	7
	pACS	4280	9
$p = 0.200$	ACS-EE	4566	10
	pACS	4565	12
$p = 0.300$	ACS-EE	5523	12
	pACS	5521	18
$p = 0.400$	ACS-EE	6252	13
	pACS	6259	13
$p = 0.500$	ACS-EE	6866	13
	pACS	6869	15

Table 24: Comparison of the average cost obtained by ACS-EE and pACS+2.5-opt-EEais over 50 homogeneous clustered instances of size 1000. Each algorithm is allowed to run for 100 CPU seconds. The table gives, for each probability level, the mean and the standard deviation (s.d.) of the final solution cost.

	Algorithm	Solution Cost	
		mean	s.d.
$p = 0.050$	ACS-EE	4147660	350857
	pACS+2.5-opt-EEais	4170183	348178
$p = 0.075$	ACS-EE	4563279	332703
	pACS+2.5-opt-EEais	4556954	341770
$p = 0.100$	ACS-EE	4971086	327017
	pACS+2.5-opt-EEais	4968883	330958
$p = 0.125$	ACS-EE	5368877	335154
	pACS+2.5-opt-EEais	5367466	326788
$p = 0.150$	ACS-EE	5742713	344837
	pACS+2.5-opt-EEais	5746223	336474
$p = 0.175$	ACS-EE	6082206	346206
	pACS+2.5-opt-EEais	6074378	346292
$p = 0.200$	ACS-EE	6399005	357165
	pACS+2.5-opt-EEais	6403956	357972
$p = 0.300$	ACS-EE	7469164	383437
	pACS+2.5-opt-EEais	7483512	388855
$p = 0.400$	ACS-EE	8338501	398825
	pACS+2.5-opt-EEais	8338545	400154
$p = 0.500$	ACS-EE	9049027	415451
	pACS+2.5-opt-EEais	9063175	409587
$p = 0.600$	ACS-EE	9656187	419358
	pACS+2.5-opt-EEais	9687613	428894
$p = 0.700$	ACS-EE	10207070	445970
	pACS+2.5-opt-EEais	10256891	440077
$p = 0.800$	ACS-EE	10682802	460677
	pACS+2.5-opt-EEais	10749186	466840
$p = 0.900$	ACS-EE	11094403	454038
	pACS+2.5-opt-EEais	11205733	474402

Table 25: Comparison of the average cost obtained by ACS-EE and pACS+2.5-opt-EEais over 50 homogeneous clustered instances of size 1000. Each algorithm is allowed to run for 1000 CPU seconds. The table gives, for each probability level, the mean and the standard deviation (s.d.) of the final solution cost.

	Algorithm	Solution Cost	
		mean	s.d.
$p = 0.050$	ACS-EE	4020924	328674
	pACS+2.5-opt-EEais	4016236	324891
$p = 0.075$	ACS-EE	4475251	319970
	pACS+2.5-opt-EEais	4474159	320366
$p = 0.100$	ACS-EE	4919834	324647
	pACS+2.5-opt-EEais	4918889	325433
$p = 0.125$	ACS-EE	5316722	332954
	pACS+2.5-opt-EEais	5314542	331382
$p = 0.150$	ACS-EE	5673340	336532
	pACS+2.5-opt-EEais	5670997	336265
$p = 0.175$	ACS-EE	6006411	347613
	pACS+2.5-opt-EEais	5999722	345234
$p = 0.200$	ACS-EE	6308767	352492
	pACS+2.5-opt-EEais	6306068	348663
$p = 0.300$	ACS-EE	7358414	366428
	pACS+2.5-opt-EEais	7360652	371075
$p = 0.400$	ACS-EE	8195261	384698
	pACS+2.5-opt-EEais	8200813	387457
$p = 0.500$	ACS-EE	8912049	402804
	pACS+2.5-opt-EEais	8916664	400761
$p = 0.600$	ACS-EE	9531201	412494
	pACS+2.5-opt-EEais	9533031	414782
$p = 0.700$	ACS-EE	10077123	424410
	pACS+2.5-opt-EEais	10086138	436974
$p = 0.800$	ACS-EE	10545376	443019
	pACS+2.5-opt-EEais	10567157	440587
$p = 0.900$	ACS-EE	10978994	447610
	pACS+2.5-opt-EEais	10995996	467494

Table 26: Comparison of the average cost obtained by ACS-EE and pACS+2.5-opt-EEais over 50 homogeneous uniform instances of size 1000. Each algorithm is allowed to run for 100 CPU seconds. The table gives, for each probability level, the mean and the standard deviation (s.d.) of the final solution cost.

	Algorithm	Solution Cost	
		mean	s.d.
$p = 0.050$	ACS-EE	6673323	68322
	pACS	6682456	74925
$p = 0.075$	ACS-EE	7899778	62675
	pACS	7899568	57722
$p = 0.100$	ACS-EE	9017943	54590
	pACS	9014007	61173
$p = 0.125$	ACS-EE	10007615	58871
	pACS	10006397	67139
$p = 0.150$	ACS-EE	10896132	74524
	pACS	10877005	73484
$p = 0.175$	ACS-EE	11687129	71896
	pACS	11680565	71793
$p = 0.200$	ACS-EE	12400133	77157
	pACS	12396764	75771
$p = 0.3$	ACS-EE	14844418	123052
	pACS	14855992	111196
$p = 0.4$	ACS-EE	16721860	142174
	pACS	16772194	124662
$p = 0.5$	ACS-EE	18285884	115986
	pACS	18331410	149276
$p = 0.6$	ACS-EE	19608813	160868
	pACS	19681795	163080
$p = 0.7$	ACS-EE	20769007	142839
	pACS	20897352	181502
$p = 0.8$	ACS-EE	21795268	196013
	pACS	21940010	169116
$p = 0.9$	ACS-EE	22669200	182924
	pACS	22881781	183177

Table 27: Comparison of the average cost obtained by ACS-EE and pACS+2.5-opt-EEais over 50 homogeneous uniform instances of size 1000. Each algorithm is allowed to run for 1000 CPU seconds. The table gives, for each probability level, the mean and the standard deviation (s.d.) of the final solution cost.

	Algorithm	Solution Cost	
		mean	s.d.
$p = 0.050$	ACS-EE	6516908	44045
	pACS	6514095	50686
$p = 0.075$	ACS-EE	7801906	52501
	pACS	7795572	53380
$p = 0.100$	ACS-EE	8912265	49076
	pACS	8906639	49546
$p = 0.125$	ACS-EE	9865815	63301
	pACS	9863972	59110
$p = 0.150$	ACS-EE	10725759	56325
	pACS	10717391	60021
$p = 0.175$	ACS-EE	11497872	69536
	pACS	11493408	64667
$p = 0.200$	ACS-EE	12207360	79765
	pACS	12210204	69590
$p = 0.3$	ACS-EE	14581882	100634
	pACS	14594081	96319
$p = 0.4$	ACS-EE	16454722	125319
	pACS	16460945	115488
$p = 0.5$	ACS-EE	18033442	131081
	pACS	18039382	129339
$p = 0.6$	ACS-EE	19375626	163644
	pACS	19395687	135667
$p = 0.7$	ACS-EE	20543279	171718
	pACS	20567909	165556
$p = 0.8$	ACS-EE	21564701	153861
	pACS	21595378	175492
$p = 0.9$	ACS-EE	22467658	185681
	pACS	22540238	190837

Table 28: Comparison of the average cost obtained by ACS-EE and pACS+2.5-opt-EEais over 50 clustered instances of size 1000.

100 CPU seconds			1000 CPU seconds		
ACS-EE vs. pACS+2.5-opt-EEais			ACS-EE vs. pACS+2.5-opt-EEais		
$p$	Difference	95% CI	$p$	Difference	95% CI
0.050	-0.540	[-1.246, +0.166]	0.050	+0.117	[-0.254, +0.488]
0.075	+0.139	[-0.458, +0.736]	0.075	+0.024	[-0.046, +0.095]
0.100	+0.044	[-0.273, +0.361]	0.100	+0.019	[-0.039, +0.077]
0.150	-0.061	[-0.392, +0.270]	0.150	+0.041	[-0.063, +0.145]
0.175	+0.129	[-0.116, +0.374]	0.175	+0.111	[-0.033, +0.256]
0.200	-0.077	[-0.389, +0.235]	0.200	+0.043	[-0.113, +0.199]
0.300	-0.192	[-0.437, +0.054]	0.300	-0.030	[-0.139, +0.078]
0.400	-0.001	[-0.209, +0.208]	0.400	-0.068	[-0.154, +0.019]
0.500	-0.156	[-0.411, +0.099]	0.500	-0.052	[-0.154, +0.050]
0.600	<b>-0.324</b>	[-0.555, -0.094]	0.600	-0.019	[-0.116, +0.077]
0.700	<b>-0.486</b>	[-0.763, -0.208]	0.700	-0.089	[-0.257, +0.078]
0.800	<b>-0.618</b>	[-0.809, -0.426]	0.800	<b>-0.206</b>	[-0.308, -0.104]
0.900	<b>-0.994</b>	[-1.221, -0.766]	0.900	<b>-0.155</b>	[-0.294, -0.015]

Table 29: Comparison of the average cost obtained by ACS-EE and pACS+2.5-opt-EEais over 50 uniform instances of size 1000.

100 CPU seconds			1000 CPU seconds		
$p$	ACS-EE vs. pACS+2.5-opt-EEais		$p$	ACS-EE vs. pACS+2.5-opt-EEais	
	Difference	95% CI		Difference	95% CI
0.050	-0.137	[-0.615, +0.341]	0.050	+0.043	[-0.206, +0.293]
0.075	+0.003	[-0.275, +0.280]	0.075	+0.081	[-0.053, +0.216]
0.100	+0.044	[-0.149, +0.237]	0.100	+0.063	[-0.041, +0.168]
0.125	+0.012	[-0.216, +0.240]	0.125	+0.019	[-0.106, +0.143]
0.150	+0.176	[-0.016, +0.367]	0.150	+0.078	[-0.039, +0.195]
0.175	+0.056	[-0.149, +0.262]	0.175	+0.039	[-0.065, +0.143]
0.200	+0.027	[-0.242, +0.296]	0.200	-0.023	[-0.151, +0.104]
0.300	-0.078	[-0.306, +0.150]	0.300	-0.084	[-0.204, +0.037]
0.400	<b>-0.300</b>	[-0.486, -0.114]	0.400	-0.038	[-0.171, +0.095]
0.500	<b>-0.248</b>	[-0.439, -0.057]	0.500	-0.033	[-0.162, +0.096]
0.600	<b>-0.371</b>	[-0.581, -0.161]	0.600	-0.103	[-0.257, +0.050]
0.700	<b>-0.614</b>	[-0.774, -0.454]	0.700	-0.120	[-0.260, +0.020]
0.800	<b>-0.660</b>	[-0.856, -0.464]	0.800	<b>-0.142</b>	[-0.261, -0.023]
0.900	<b>-0.929</b>	[-1.102, -0.756]	0.900	<b>-0.322</b>	[-0.463, -0.181]

### **3 Comparison between the estimation-based ACO variants**

### **3.1 Comparison between the variants with default parameter values**

Table 30: The average and the standard deviation of the cost obtained by ACS-EE(d), MMAS-EE(d), RAS-EE(d), and BWAS-EE(d), on the TSPLIB instance ch150 for  $n^2/10000$  CPU seconds. The statistics is computed over 30 runs.

		Algorithm	Solution Cost
		mean	s.d.
$p = 0.050$	MMAS-EE(t)	1774	2
	ACS-EE(t)	1774	2
	RAS-EE(t)	1773	2
	BWAS-EE(t)	1774	2
$p = 0.075$	MMAS-EE(t)	2166	2
	ACS-EE(t)	2167	2
	RAS-EE(t)	2166	1
	BWAS-EE(t)	2167	1
$p = 0.100$	MMAS-EE(t)	2486	2
	ACS-EE(t)	2490	4
	RAS-EE(t)	2488	3
	BWAS-EE(t)	2487	2
$p = 0.150$	MMAS-EE(t)	3036	12
	ACS-EE(t)	3044	12
	RAS-EE(t)	3038	12
	BWAS-EE(t)	3037	11
$p = 0.175$	MMAS-EE(t)	3272	12
	ACS-EE(t)	3276	18
	RAS-EE(t)	3275	17
	BWAS-EE(t)	3271	11
$p = 0.200$	MMAS-EE(t)	3465	14
	ACS-EE(t)	3472	17
	RAS-EE(t)	3469	16
	BWAS-EE(t)	3469	18
$p = 0.300$	MMAS-EE(t)	4169	39
	ACS-EE(t)	4160	39
	RAS-EE(t)	4162	29
	BWAS-EE(t)	4160	36
$p = 0.400$	MMAS-EE(t)	4751	63
	ACS-EE(t)	4724	45
	RAS-EE(t)	4748	44
	BWAS-EE(t)	4756	45
$p = 0.500$	MMAS-EE(t)	5262	53
	ACS-EE(t)	5181	68
	RAS-EE(t)	5268	58
	BWAS-EE(t)	5244	53

Table 31: The average and the standard deviation of the cost obtained by ACS-EE(d), MMAS-EE(d), RAS-EE(d), and BWAS-EE(d), on the TSPLIB instance ch150 for  $n^2/1000$  CPU seconds. The statistics is computed over 30 runs.

		Algorithm	Solution Cost
		mean	s.d.
$p = 0.050$	MMAS-EE(t)	1773	1
	ACS-EE(t)	1773	1
	RAS-EE(t)	1773	1
	BWAS-EE(t)	1773	1
$p = 0.075$	MMAS-EE(t)	2166	1
	ACS-EE(t)	2167	1
	RAS-EE(t)	2166	1
	BWAS-EE(t)	2167	1
$p = 0.100$	MMAS-EE(t)	2487	2
	ACS-EE(t)	2489	3
	RAS-EE(t)	2487	2
	BWAS-EE(t)	2487	1
$p = 0.150$	MMAS-EE(t)	3019	3
	ACS-EE(t)	3015	1
	RAS-EE(t)	3019	2
	BWAS-EE(t)	3016	1
$p = 0.175$	MMAS-EE(t)	3247	5
	ACS-EE(t)	3242	3
	RAS-EE(t)	3250	5
	BWAS-EE(t)	3242	3
$p = 0.200$	MMAS-EE(t)	3422	2
	ACS-EE(t)	3422	5
	RAS-EE(t)	3433	4
	BWAS-EE(t)	3422	4
$p = 0.300$	MMAS-EE(t)	4059	6
	ACS-EE(t)	4062	9
	RAS-EE(t)	4083	8
	BWAS-EE(t)	4059	6
$p = 0.400$	MMAS-EE(t)	4577	10
	ACS-EE(t)	4579	13
	RAS-EE(t)	4581	9
	BWAS-EE(t)	4578	12
$p = 0.500$	MMAS-EE(t)	5007	7
	ACS-EE(t)	5008	9
	RAS-EE(t)	5006	5
	BWAS-EE(t)	5010	12

Table 32: The average and the standard deviation of the cost obtained by ACS-EE(d), MMAS-EE(d), RAS-EE(d), and BWAS-EE(d), on the TSPLIB instance d198 for  $n^2/10000$  CPU seconds. The statistics is computed over 30 runs.

		Algorithm	Solution Cost	
			mean	s.d.
$p = 0.050$	MMAS-EE(t)	5633	22	
	ACS-EE(t)	5631	14	
	RAS-EE(t)	5632	18	
	BWAS-EE(t)	5638	24	
$p = 0.075$	MMAS-EE(t)	6677	2	
	ACS-EE(t)	6678	3	
	RAS-EE(t)	6677	2	
	BWAS-EE(t)	6677	1	
$p = 0.100$	MMAS-EE(t)	7447	3	
	ACS-EE(t)	7451	6	
	RAS-EE(t)	7449	3	
	BWAS-EE(t)	7448	4	
$p = 0.150$	MMAS-EE(t)	8567	14	
	ACS-EE(t)	8567	16	
	RAS-EE(t)	8572	13	
	BWAS-EE(t)	8563	12	
$p = 0.175$	MMAS-EE(t)	8999	20	
	ACS-EE(t)	8998	25	
	RAS-EE(t)	9002	20	
	BWAS-EE(t)	8993	19	
$p = 0.200$	MMAS-EE(t)	9399	28	
	ACS-EE(t)	9390	35	
	RAS-EE(t)	9387	23	
	BWAS-EE(t)	9389	31	
$p = 0.300$	MMAS-EE(t)	10705	41	
	ACS-EE(t)	10713	45	
	RAS-EE(t)	10701	43	
	BWAS-EE(t)	10696	49	
$p = 0.400$	MMAS-EE(t)	11764	58	
	ACS-EE(t)	11768	48	
	RAS-EE(t)	11782	49	
	BWAS-EE(t)	11772	55	
$p = 0.500$	MMAS-EE(t)	12684	60	
	ACS-EE(t)	12689	77	
	RAS-EE(t)	12739	58	
	BWAS-EE(t)	12711	60	

Table 33: The average and the standard deviation of the cost obtained by ACS-EE(d), MMAS-EE(d), RAS-EE(d), and BWAS-EE(d), on the TSPLIB instance d198 for  $n^2/1000$  CPU seconds. The statistics is computed over 30 runs.

		Algorithm	Solution Cost	
			mean	s.d.
$p = 0.050$	MMAS-EE(t)	5611	1	
	ACS-EE(t)	5612	1	
	RAS-EE(t)	5612	1	
	BWAS-EE(t)	5612	1	
$p = 0.075$	MMAS-EE(t)	6678	2	
	ACS-EE(t)	6679	3	
	RAS-EE(t)	6677	2	
	BWAS-EE(t)	6678	2	
$p = 0.100$	MMAS-EE(t)	7447	4	
	ACS-EE(t)	7450	5	
	RAS-EE(t)	7448	3	
	BWAS-EE(t)	7448	6	
$p = 0.150$	MMAS-EE(t)	8538	4	
	ACS-EE(t)	8534	2	
	RAS-EE(t)	8540	4	
	BWAS-EE(t)	8535	2	
$p = 0.175$	MMAS-EE(t)	8952	3	
	ACS-EE(t)	8948	3	
	RAS-EE(t)	8958	4	
	BWAS-EE(t)	8949	3	
$p = 0.200$	MMAS-EE(t)	9327	3	
	ACS-EE(t)	9325	3	
	RAS-EE(t)	9334	4	
	BWAS-EE(t)	9325	3	
$p = 0.300$	MMAS-EE(t)	10550	6	
	ACS-EE(t)	10546	5	
	RAS-EE(t)	10583	12	
	BWAS-EE(t)	10548	6	
$p = 0.400$	MMAS-EE(t)	11546	6	
	ACS-EE(t)	11546	12	
	RAS-EE(t)	11600	15	
	BWAS-EE(t)	11548	9	
$p = 0.500$	MMAS-EE(t)	12425	5	
	ACS-EE(t)	12427	4	
	RAS-EE(t)	12468	18	
	BWAS-EE(t)	12425	5	

Table 34: The average and the standard deviation of the cost obtained by ACS-EE(d), MMAS-EE(d), RAS-EE(d), and BWAS-EE(d), on the TSPLIB instance lin318 for  $n^2/10000$  CPU seconds. The statistics is computed over 30 runs.

		Algorithm	Solution Cost
		mean	s.d.
$p = 0.050$	MMAS-EE(d)	12708	54
	ACS-EE(d)	12689	59
	RAS-EE(d)	12699	88
	BWAS-EE(d)	12713	88
$p = 0.075$	MMAS-EE(d)	15225	139
	ACS-EE(d)	15223	128
	RAS-EE(d)	15199	81
	BWAS-EE(d)	15201	99
$p = 0.100$	MMAS-EE(d)	17330	76
	ACS-EE(d)	17395	109
	RAS-EE(d)	17318	60
	BWAS-EE(d)	17348	75
$p = 0.150$	MMAS-EE(d)	21151	142
	ACS-EE(d)	21404	229
	RAS-EE(d)	21145	147
	BWAS-EE(d)	21150	106
$p = 0.175$	MMAS-EE(d)	22787	250
	ACS-EE(d)	22982	213
	RAS-EE(d)	22712	229
	BWAS-EE(d)	22781	202
$p = 0.200$	MMAS-EE(d)	24287	229
	ACS-EE(d)	24474	213
	RAS-EE(d)	24294	188
	BWAS-EE(d)	24307	243
$p = 0.300$	MMAS-EE(d)	29173	205
	ACS-EE(d)	29048	194
	RAS-EE(d)	29089	282
	BWAS-EE(d)	29168	245
$p = 0.400$	MMAS-EE(d)	32910	291
	ACS-EE(d)	32413	238
	RAS-EE(d)	32878	319
	BWAS-EE(d)	32896	375
$p = 0.500$	MMAS-EE(d)	35959	336
	ACS-EE(d)	35236	299
	RAS-EE(d)	35913	359
	BWAS-EE(d)	35952	366

Table 35: The average and the standard deviation of the cost obtained by ACS-EE(d), MMAS-EE(d), RAS-EE(d), and BWAS-EE(d), on the TSPLIB instance lin318 for  $n^2/1000$  CPU seconds. The statistics is computed over 30 runs.

		Algorithm	Solution Cost
		mean	s.d.
$p = 0.050$	MMAS-EE(d)	12622	20
	ACS-EE(d)	12627	22
	RAS-EE(d)	12621	19
	BWAS-EE(d)	12621	26
$p = 0.075$	MMAS-EE(d)	15112	15
	ACS-EE(d)	15110	11
	RAS-EE(d)	15110	11
	BWAS-EE(d)	15110	10
$p = 0.100$	MMAS-EE(d)	17250	17
	ACS-EE(d)	17226	10
	RAS-EE(d)	17244	16
	BWAS-EE(d)	17233	9
$p = 0.150$	MMAS-EE(d)	20805	35
	ACS-EE(d)	20744	50
	RAS-EE(d)	20871	42
	BWAS-EE(d)	20775	44
$p = 0.175$	MMAS-EE(d)	22281	44
	ACS-EE(d)	22224	56
	RAS-EE(d)	22369	58
	BWAS-EE(d)	22247	53
$p = 0.200$	MMAS-EE(d)	23578	55
	ACS-EE(d)	23548	111
	RAS-EE(d)	23745	93
	BWAS-EE(d)	23544	80
$p = 0.300$	MMAS-EE(d)	27954	155
	ACS-EE(d)	27991	121
	RAS-EE(d)	28395	100
	BWAS-EE(d)	27966	143
$p = 0.400$	MMAS-EE(d)	31232	97
	ACS-EE(d)	31230	83
	RAS-EE(d)	31726	81
	BWAS-EE(d)	31301	134
$p = 0.500$	MMAS-EE(d)	33884	82
	ACS-EE(d)	33885	103
	RAS-EE(d)	34421	102
	BWAS-EE(d)	33901	76

Table 36: The average and the standard deviation of the cost obtained by ACS-EE(d), MMAS-EE(d), RAS-EE(d), and BWAS-EE(d), on the TSPLIB instance att532 for  $n^2/10000$  CPU seconds. The statistics is computed over 30 runs.

		Algorithm	Solution Cost
		mean	s.d.
$p = 0.050$	MMAS-EE(d)	25857	177
	ACS-EE(d)	25871	214
	RAS-EE(d)	25893	149
	BWAS-EE(d)	25818	138
$p = 0.075$	MMAS-EE(d)	30133	78
	ACS-EE(d)	30150	106
	RAS-EE(d)	30149	129
	BWAS-EE(d)	30132	92
$p = 0.100$	MMAS-EE(d)	33980	126
	ACS-EE(d)	34081	168
	RAS-EE(d)	33960	117
	BWAS-EE(d)	33967	102
$p = 0.150$	MMAS-EE(d)	40583	219
	ACS-EE(d)	40972	307
	RAS-EE(d)	40591	195
	BWAS-EE(d)	40549	205
$p = 0.175$	MMAS-EE(d)	43488	284
	ACS-EE(d)	43960	388
	RAS-EE(d)	43490	195
	BWAS-EE(d)	43433	216
$p = 0.200$	MMAS-EE(d)	46136	257
	ACS-EE(d)	46864	394
	RAS-EE(d)	46107	299
	BWAS-EE(d)	46215	273
$p = 0.300$	MMAS-EE(d)	55639	356
	ACS-EE(d)	56330	463
	RAS-EE(d)	55515	472
	BWAS-EE(d)	55661	414
$p = 0.400$	MMAS-EE(d)	63184	476
	ACS-EE(d)	63790	409
	RAS-EE(d)	63422	404
	BWAS-EE(d)	63209	507
$p = 0.500$	MMAS-EE(d)	70182	445
	ACS-EE(d)	70232	469
	RAS-EE(d)	70190	576
	BWAS-EE(d)	69986	583

Table 37: The average and the standard deviation of the cost obtained by ACS-EE(d), MMAS-EE(d), RAS-EE(d), and BWAS-EE(d), on the TSPLIB instance att532 for  $n^2/1000$  CPU seconds. The statistics is computed over 30 runs.

		Algorithm	Solution Cost
		mean	s.d.
$p = 0.050$	MMAS-EE(d)	25621	60
	ACS-EE(d)	25548	19
	RAS-EE(d)	25595	38
	BWAS-EE(d)	25544	18
$p = 0.075$	MMAS-EE(d)	30022	26
	ACS-EE(d)	29994	17
	RAS-EE(d)	30022	21
	BWAS-EE(d)	30008	16
$p = 0.100$	MMAS-EE(d)	33823	33
	ACS-EE(d)	33749	21
	RAS-EE(d)	33838	43
	BWAS-EE(d)	33791	30
$p = 0.150$	MMAS-EE(d)	39947	68
	ACS-EE(d)	39777	32
	RAS-EE(d)	40165	99
	BWAS-EE(d)	39865	60
$p = 0.175$	MMAS-EE(d)	42555	96
	ACS-EE(d)	42366	71
	RAS-EE(d)	42912	82
	BWAS-EE(d)	42465	58
$p = 0.200$	MMAS-EE(d)	44981	97
	ACS-EE(d)	44763	63
	RAS-EE(d)	45525	90
	BWAS-EE(d)	44854	87
$p = 0.300$	MMAS-EE(d)	53310	127
	ACS-EE(d)	53217	134
	RAS-EE(d)	54411	181
	BWAS-EE(d)	53303	178
$p = 0.400$	MMAS-EE(d)	60132	171
	ACS-EE(d)	60162	186
	RAS-EE(d)	61484	147
	BWAS-EE(d)	60229	164
$p = 0.500$	MMAS-EE(d)	66170	106
	ACS-EE(d)	66253	127
	RAS-EE(d)	67762	173
	BWAS-EE(d)	66308	212

Table 38: The average and the standard deviation of the cost obtained by ACS-EE(d), MMAS-EE(d), RAS-EE(d), and BWAS-EE(d), on the TSPLIB instance rat783 for  $n^2/10000$  CPU seconds. The statistics is computed over 30 runs.

		Algorithm	Solution	Cost
			mean	s.d.
$p = 0.050$	MMAS-EE(d)	2357	11	
	ACS-EE(d)	2361	17	
	RAS-EE(d)	2360	10	
	BWAS-EE(d)	2361	12	
$p = 0.075$	MMAS-EE(d)	2862	11	
	ACS-EE(d)	2858	10	
	RAS-EE(d)	2864	10	
	BWAS-EE(d)	2864	13	
$p = 0.100$	MMAS-EE(d)	3289	7	
	ACS-EE(d)	3301	9	
	RAS-EE(d)	3288	8	
	BWAS-EE(d)	3288	11	
$p = 0.150$	MMAS-EE(d)	4047	16	
	ACS-EE(d)	4086	17	
	RAS-EE(d)	4053	12	
	BWAS-EE(d)	4052	12	
$p = 0.175$	MMAS-EE(d)	4386	13	
	ACS-EE(d)	4432	23	
	RAS-EE(d)	4387	14	
	BWAS-EE(d)	4393	14	
$p = 0.200$	MMAS-EE(d)	4700	15	
	ACS-EE(d)	4751	27	
	RAS-EE(d)	4699	15	
	BWAS-EE(d)	4698	16	
$p = 0.300$	MMAS-EE(d)	5768	24	
	ACS-EE(d)	5814	28	
	RAS-EE(d)	5769	29	
	BWAS-EE(d)	5778	23	
$p = 0.400$	MMAS-EE(d)	6609	32	
	ACS-EE(d)	6597	23	
	RAS-EE(d)	6607	25	
	BWAS-EE(d)	6613	36	
$p = 0.500$	MMAS-EE(d)	7309	34	
	ACS-EE(d)	7227	34	
	RAS-EE(d)	7305	35	
	BWAS-EE(d)	7307	28	

Table 39: The average and the standard deviation of the cost obtained by ACS-EE(d), MMAS-EE(d), RAS-EE(d), and BWAS-EE(d), on the TSPLIB instance rat783 for  $n^2/1000$  CPU seconds. The statistics is computed over 30 runs.

		Algorithm	Solution Cost
		mean	s.d.
$p = 0.050$	MMAS-EE(d)	2341	6
	ACS-EE(d)	2332	4
	RAS-EE(d)	2340	4
	BWAS-EE(d)	2334	5
$p = 0.075$	MMAS-EE(d)	2844	6
	ACS-EE(d)	2832	6
	RAS-EE(d)	2840	5
	BWAS-EE(d)	2836	5
$p = 0.100$	MMAS-EE(d)	3276	6
	ACS-EE(d)	3264	6
	RAS-EE(d)	3278	7
	BWAS-EE(d)	3269	6
$p = 0.150$	MMAS-EE(d)	4010	10
	ACS-EE(d)	3969	9
	RAS-EE(d)	4033	10
	BWAS-EE(d)	3996	9
$p = 0.175$	MMAS-EE(d)	4324	13
	ACS-EE(d)	4280	8
	RAS-EE(d)	4368	9
	BWAS-EE(d)	4304	14
$p = 0.200$	MMAS-EE(d)	4611	17
	ACS-EE(d)	4563	11
	RAS-EE(d)	4674	9
	BWAS-EE(d)	4593	12
$p = 0.300$	MMAS-EE(d)	5559	20
	ACS-EE(d)	5515	17
	RAS-EE(d)	5711	10
	BWAS-EE(d)	5541	15
$p = 0.400$	MMAS-EE(d)	6268	13
	ACS-EE(d)	6246	14
	RAS-EE(d)	6483	16
	BWAS-EE(d)	6275	15
$p = 0.500$	MMAS-EE(d)	6871	14
	ACS-EE(d)	6872	15
	RAS-EE(d)	7120	15
	BWAS-EE(d)	6890	15

Table 40: The average and the standard deviation of the cost obtained by ACS-EE(d), MMAS-EE(d), RAS-EE(d), and BWAS-EE(d), on the clustered instances of size 1000 for 100 seconds. The statistics is computed over 50 instances.

		Algorithm	Solution Cost	
			mean	s.d.
$p = 0.050$	MMAS-EE(d)	4374698	446663	
	ACS-EE(d)	4491475	472454	
	RAS-EE(d)	4427947	502224	
	BWAS-EE(d)	4458108	479762	
$p = 0.075$	MMAS-EE(d)	4757749	448712	
	ACS-EE(d)	4622715	432053	
	RAS-EE(d)	4786247	460180	
	BWAS-EE(d)	4772766	422401	
$p = 0.100$	MMAS-EE(d)	5139042	457430	
	ACS-EE(d)	4938350	427685	
	RAS-EE(d)	5020786	443524	
	BWAS-EE(d)	4991101	457574	
$p = 0.125$	MMAS-EE(d)	5375411	440664	
	ACS-EE(d)	5322564	430118	
	RAS-EE(d)	5349909	434020	
	BWAS-EE(d)	5329998	440454	
$p = 0.150$	MMAS-EE(d)	5737006	454071	
	ACS-EE(d)	5697048	442312	
	RAS-EE(d)	5731734	452556	
	BWAS-EE(d)	5703725	445289	
$p = 0.175$	MMAS-EE(d)	6089386	462871	
	ACS-EE(d)	6026438	461995	
	RAS-EE(d)	6086602	454819	
	BWAS-EE(d)	6051701	450660	
$p = 0.200$	MMAS-EE(d)	6418386	467346	
	ACS-EE(d)	6343778	465912	
	RAS-EE(d)	6413096	474335	
	BWAS-EE(d)	6377132	460499	
$p = 0.300$	MMAS-EE(d)	7565140	511879	
	ACS-EE(d)	7395142	495970	
	RAS-EE(d)	7547226	503640	
	BWAS-EE(d)	7483040	514697	
$p = 0.400$	MMAS-EE(d)	8467527	543114	
	ACS-EE(d)	8204142	531915	
	RAS-EE(d)	8447704	544122	
	BWAS-EE(d)	8336366	544197	
$p = 0.500$	MMAS-EE(d)	9184723	572314	
	ACS-EE(d)	8879886	553487	
	RAS-EE(d)	9182258	577258	
	BWAS-EE(d)	9035761	566633	
$p = 0.600$	MMAS-EE(d)	9797965	602129	
	ACS-EE(d)	9478634	585929	
	RAS-EE(d)	9829753	603344	
	BWAS-EE(d)	9640730	592668	

Table 41: The average and the standard deviation of the cost obtained by ACS-EE(d), MMAS-EE(d), RAS-EE(d), and BWAS-EE(d), on the clustered instances of size 1000 for 1000 seconds. The statistics is computed over 50 instances.

		Algorithm	Solution Cost	
			mean	s.d.
$p = 0.050$	MMAS-EE(d)	4074972	407949	
	ACS-EE(d)	3997851	398735	
	RAS-EE(d)	4041347	401461	
	BWAS-EE(d)	4034365	403323	
$p = 0.075$	MMAS-EE(d)	4521857	411328	
	ACS-EE(d)	4440309	403161	
	RAS-EE(d)	4502017	410769	
	BWAS-EE(d)	4477324	412996	
$p = 0.100$	MMAS-EE(d)	4909640	421732	
	ACS-EE(d)	4873033	415815	
	RAS-EE(d)	4907397	418015	
	BWAS-EE(d)	4891545	419359	
$p = 0.125$	MMAS-EE(d)	5294843	430150	
	ACS-EE(d)	5260257	427569	
	RAS-EE(d)	5303968	426121	
	BWAS-EE(d)	5282804	431738	
$p = 0.150$	MMAS-EE(d)	5656771	438786	
	ACS-EE(d)	5612055	436792	
	RAS-EE(d)	5683764	444281	
	BWAS-EE(d)	5643998	440801	
$p = 0.175$	MMAS-EE(d)	5988978	454070	
	ACS-EE(d)	5933596	448004	
	RAS-EE(d)	6038521	451957	
	BWAS-EE(d)	5966562	449636	
$p = 0.200$	MMAS-EE(d)	6291929	456447	
	ACS-EE(d)	6231764	457752	
	RAS-EE(d)	6366718	467615	
	BWAS-EE(d)	6260014	460287	
$p = 0.300$	MMAS-EE(d)	7298438	497878	
	ACS-EE(d)	7253328	492006	
	RAS-EE(d)	7492238	500245	
	BWAS-EE(d)	7273365	491953	
$p = 0.400$	MMAS-EE(d)	8091205	525116	
	ACS-EE(d)	8072577	519518	
	RAS-EE(d)	8374745	539255	
	BWAS-EE(d)	8096180	518896	
$p = 0.500$	MMAS-EE(d)	8778254	545685	
	ACS-EE(d)	8766055	539932	
	RAS-EE(d)	9121760	567788	
	BWAS-EE(d)	8801746	542085	
$p = 0.600$	MMAS-EE(d)	9375577	572045	
	ACS-EE(d)	9381698	572438	
	RAS-EE(d)	9760497	604534	
	BWAS-EE(d)	9398013	567083	

Table 42: The average and the standard deviation of the cost obtained by ACS-EE(d), MMAS-EE(d), RAS-EE(d), and BWAS-EE(d), on the uniform instances of size 1000 for  $n^2/10000$  CPU seconds. The statistics is computed over 50 instances.

		Algorithm	Solution Cost	
			mean	s.d.
$p = 0.050$		MMAS-EE(d)	6910763	77425
		ACS-EE(d)	7034406	206422
		RAS-EE(d)	6933591	121310
		BWAS-EE(d)	6974971	133203
$p = 0.075$		MMAS-EE(d)	8236144	82097
		ACS-EE(d)	8032349	78886
		RAS-EE(d)	8237148	89213
		BWAS-EE(d)	8239246	86588
$p = 0.100$		MMAS-EE(d)	9241282	67287
		ACS-EE(d)	9037977	63581
		RAS-EE(d)	9123181	68244
		BWAS-EE(d)	9057788	71417
$p = 0.125$		MMAS-EE(d)	10089500	75232
		ACS-EE(d)	10049148	76289
		RAS-EE(d)	10095539	74824
		BWAS-EE(d)	10037175	69019
$p = 0.150$		MMAS-EE(d)	11022201	78937
		ACS-EE(d)	10936072	83677
		RAS-EE(d)	11024829	78699
		BWAS-EE(d)	10942533	76964
$p = 0.175$		MMAS-EE(d)	11854754	94655
		ACS-EE(d)	11740364	97578
		RAS-EE(d)	11869620	78995
		BWAS-EE(d)	11770992	83194
$p = 0.200$		MMAS-EE(d)	12624614	93861
		ACS-EE(d)	12463098	96886
		RAS-EE(d)	12648742	85037
		BWAS-EE(d)	12527787	96416
$p = 0.3$		MMAS-EE(d)	15292164	100621
		ACS-EE(d)	14854118	113898
		RAS-EE(d)	15286445	110945
		BWAS-EE(d)	15093020	130972
$p = 0.4$		MMAS-EE(d)	17288833	123504
		ACS-EE(d)	16693966	151786
		RAS-EE(d)	17276006	124855
		BWAS-EE(d)	17008296	159686
$p = 0.5$		MMAS-EE(d)	18881810	149761
		ACS-EE(d)	18223264	148396
		RAS-EE(d)	18901545	156115
		BWAS-EE(d)	18557754	173131
$p = 0.6$		MMAS-EE(d)	20161721	182699
		ACS-EE(d)	19566148	200112
		RAS-EE(d)	20284133	151956
		BWAS-EE(d)	19817599	209563

Table 43: The average and the standard deviation of the cost obtained by ACS-EE(d), MMAS-EE(d), RAS-EE(d), and BWAS-EE(d), on the uniform instances of size 1000 for  $n^2/1000$  CPU seconds. The statistics is computed over 50 instances.

		Algorithm	Solution Cost	
			mean	s.d.
$p = 0.050$	MMAS-EE(d)	6682762	58494	
	ACS-EE(d)	6549876	50964	
	RAS-EE(d)	6660497	51823	
	BWAS-EE(d)	6622664	50109	
$p = 0.075$	MMAS-EE(d)	7925778	59502	
	ACS-EE(d)	7816906	60248	
	RAS-EE(d)	7917664	59578	
	BWAS-EE(d)	7863756	68082	
$p = 0.100$	MMAS-EE(d)	9014820	63187	
	ACS-EE(d)	8929585	64418	
	RAS-EE(d)	9029225	65786	
	BWAS-EE(d)	8982451	64449	
$p = 0.125$	MMAS-EE(d)	9972863	76419	
	ACS-EE(d)	9876558	76555	
	RAS-EE(d)	10046530	69172	
	BWAS-EE(d)	9940088	71044	
$p = 0.150$	MMAS-EE(d)	10838446	83344	
	ACS-EE(d)	10729050	75049	
	RAS-EE(d)	10973762	79324	
	BWAS-EE(d)	10789411	83792	
$p = 0.175$	MMAS-EE(d)	11606302	96657	
	ACS-EE(d)	11496403	80536	
	RAS-EE(d)	11819450	79740	
	BWAS-EE(d)	11554946	85361	
$p = 0.200$	MMAS-EE(d)	12303276	91345	
	ACS-EE(d)	12203897	85471	
	RAS-EE(d)	12584507	81043	
	BWAS-EE(d)	12257889	88911	
$p = 0.3$	MMAS-EE(d)	14631137	102982	
	ACS-EE(d)	14585849	115694	
	RAS-EE(d)	15186177	100150	
	BWAS-EE(d)	14629375	109135	
$p = 0.4$	MMAS-EE(d)	16461778	121859	
	ACS-EE(d)	16459537	131996	
	RAS-EE(d)	17175858	130372	
	BWAS-EE(d)	16514221	130254	
$p = 0.5$	MMAS-EE(d)	18012458	137699	
	ACS-EE(d)	18044999	151848	
	RAS-EE(d)	18786128	144401	
	BWAS-EE(d)	18074489	139540	
$p = 0.6$	MMAS-EE(d)	19362035	161423	
	ACS-EE(d)	19388889	159717	
	RAS-EE(d)	20171457	181809	
	BWAS-EE(d)	19418631	178390	

Table 44: Comparison of the average cost obtained by ACS-EE(d), MMAS-EE(d), RAS-EE(d), and BWAS-EE(d) over 30 independent runs on instance lin318.

$n^2/10000$ CPU seconds						
	ACS-EE(d) vs. MMAS-EE(d)		ACS-EE(d) vs. RAS-EE(d)		ACS-EE(d) vs. BWAS-EE(d)	
$p$	Difference	95% CI	Difference	95% CI	Difference	95% CI
0.050-00	-0.139	[-0.417, +0.140]	-0.107	[-0.447, +0.233]	-0.185	[-0.565, +0.196]
0.075-00	-0.018	[-0.651, +0.616]	+0.224	[-0.219, +0.667]	+0.211	[-0.332, +0.754]
0.100-00	+0.443	[+0.129, +0.756]	+0.526	[+0.257, +0.794]	+0.360	[+0.079, +0.641]
0.150-00	+1.168	[+0.678, +1.658]	+1.225	[+0.752, +1.697]	+1.175	[+0.744, +1.606]
0.175-00	+0.852	[+0.269, +1.434]	+1.188	[+0.688, +1.688]	+0.879	[+0.357, +1.401]
0.200-00	+0.771	[+0.333, +1.210]	+0.743	[+0.303, +1.183]	+0.644	[+0.068, +1.219]
0.300-00	-0.503	[-0.887, -0.118]	-0.154	[-0.641, +0.332]	-0.413	[-0.876, +0.050]
0.400-00	-1.511	[-1.953, -1.069]	-1.457	[-1.914, -0.999]	-1.469	[-1.990, -0.947]
0.500-00	-2.012	[-2.484, -1.539]	-1.886	[-2.439, -1.334]	-1.986	[-2.516, -1.456]

  

$n^2/1000$ CPU seconds						
	ACS-EE(d) vs. MMAS-EE(d)		ACS-EE(d) vs. RAS-EE(d)		ACS-EE(d) vs. BWAS-EE(d)	
$p$	Difference	95% CI	Difference	95% CI	Difference	95% CI
0.050-00	+0.024	[-0.079, +0.127]	+0.045	[-0.073, +0.163]	+0.024	[-0.109, +0.156]
0.075-00	-0.025	[-0.078, +0.028]	+0.000	[-0.056, +0.056]	+0.000	[-0.054, +0.054]
0.100-00	-0.167	[-0.220, -0.114]	-0.128	[-0.186, -0.069]	-0.051	[-0.093, -0.010]
0.150-00	-0.237	[-0.383, -0.091]	-0.574	[-0.739, -0.410]	-0.086	[-0.221, +0.048]
0.175-00	-0.228	[-0.371, -0.084]	-0.620	[-0.763, -0.478]	-0.056	[-0.238, +0.126]
0.200-00	-0.086	[-0.308, +0.136]	-0.826	[-1.060, -0.592]	+0.035	[-0.194, +0.263]
0.300-00	+0.088	[-0.281, +0.458]	-1.424	[-1.667, -1.181]	+0.091	[-0.237, +0.419]
0.400-00	+0.014	[-0.141, +0.170]	-1.551	[-1.732, -1.371]	-0.200	[-0.416, +0.016]
0.500-00	+0.039	[-0.103, +0.180]	-1.535	[-1.720, -1.351]	-0.034	[-0.190, +0.123]

Table 45: Comparison of the average cost obtained by ACS-EE(d), MMAS-EE(d), RAS-EE(d), and BWAS-EE(d) over 30 independent runs on instance att532.

$n^2/10000$ CPU seconds						
	ACS-EE(d) vs. MMAS-EE(d)		ACS-EE(d) vs. RAS-EE(d)		ACS-EE(d) vs. BWAS-EE(d)	
$p$	Difference	95% CI	Difference	95% CI	Difference	95% CI
0.050-00	+0.172	[−0.274, +0.618]	−0.034	[−0.426, +0.358]	+0.253	[−0.177, +0.684]
0.075-00	+0.094	[−0.107, +0.295]	+0.007	[−0.247, +0.262]	+0.063	[−0.107, +0.233]
0.100-00	+0.371	[+0.127, +0.615]	+0.383	[+0.159, +0.606]	+0.347	[+0.120, +0.575]
0.150-00	+0.957	[+0.639, +1.276]	+0.949	[+0.634, +1.265]	+1.042	[+0.677, +1.407]
0.175-00	+1.085	[+0.716, +1.454]	+1.082	[+0.713, +1.452]	+1.205	[+0.771, +1.639]
0.200-00	+1.622	[+1.268, +1.976]	+1.673	[+1.219, +2.127]	+1.433	[+0.994, +1.872]
0.300-00	+1.274	[+0.811, +1.737]	+1.505	[+1.094, +1.916]	+1.186	[+0.785, +1.586]
0.400-00	+0.959	[+0.584, +1.334]	+0.580	[+0.259, +0.901]	+0.918	[+0.500, +1.337]
0.500-00	+0.121	[−0.324, +0.566]	+0.082	[−0.268, +0.432]	+0.364	[−0.015, +0.742]

  

$n^2/1000$ CPU seconds						
	ACS-EE(d) vs. MMAS-EE(d)		ACS-EE(d) vs. RAS-EE(d)		ACS-EE(d) vs. BWAS-EE(d)	
$p$	Difference	95% CI	Difference	95% CI	Difference	95% CI
0.050-00	<b>−0.284</b>	[−0.393, −0.175]	<b>−0.177</b>	[−0.248, −0.107]	+0.022	[−0.029, +0.073]
0.075-00	<b>−0.099</b>	[−0.137, −0.061]	<b>−0.095</b>	[−0.136, −0.054]	<b>−0.049</b>	[−0.086, −0.013]
0.100-00	<b>−0.194</b>	[−0.240, −0.148]	<b>−0.269</b>	[−0.332, −0.206]	<b>−0.126</b>	[−0.175, −0.077]
0.150-00	<b>−0.433</b>	[−0.510, −0.356]	<b>−0.979</b>	[−1.093, −0.865]	<b>−0.216</b>	[−0.287, −0.144]
0.175-00	<b>−0.446</b>	[−0.572, −0.321]	<b>−1.245</b>	[−1.346, −1.144]	<b>−0.222</b>	[−0.299, −0.146]
0.200-00	<b>−0.492</b>	[−0.607, −0.378]	<b>−1.652</b>	[−1.758, −1.546]	<b>−0.198</b>	[−0.301, −0.096]
0.300-00	<b>−0.175</b>	[−0.299, −0.050]	<b>−2.194</b>	[−2.345, −2.044]	−0.160	[−0.333, +0.012]
0.400-00	+0.024	[−0.149, +0.197]	<b>−2.174</b>	[−2.320, −2.028]	−0.119	[−0.266, +0.028]
0.500-00	+0.126	[+0.035, +0.218]	<b>−2.217</b>	[−2.346, −2.088]	−0.105	[−0.269, +0.060]

Table 46: Comparison of the average cost obtained by ACS-EE(d), MMAS-EE(d), RAS-EE(d), and BWAS-EE(d) over 30 independent runs on instance rat783.

$n^2/10000$ CPU seconds						
	ACS-EE(d) vs. MMAS-EE(d)		ACS-EE(d) vs. RAS-EE(d)		ACS-EE(d) vs. BWAS-EE(d)	
$p$	Difference	95% CI	Difference	95% CI	Difference	95% CI
0.050-00	+0.117	[−0.338, +0.572]	+0.148	[−0.271, +0.568]	−0.105	[−0.494, +0.284]
0.075-00	−0.159	[−0.424, +0.106]	−0.183	[−0.394, +0.027]	−0.171	[−0.414, +0.071]
0.100-00	+0.397	[+0.195, +0.599]	+0.372	[+0.165, +0.579]	+0.472	[+0.232, +0.711]
0.150-00	+0.996	[+0.731, +1.261]	+0.809	[+0.575, +1.043]	+0.758	[+0.483, +1.034]
0.175-00	+1.027	[+0.753, +1.301]	+1.020	[+0.754, +1.286]	+0.905	[+0.635, +1.175]
0.200-00	+1.009	[+0.736, +1.281]	+1.046	[+0.752, +1.341]	+1.055	[+0.758, +1.352]
0.300-00	+0.808	[+0.549, +1.066]	+0.802	[+0.465, +1.140]	+0.638	[+0.392, +0.885]
0.400-00	−0.136	[−0.368, +0.097]	−0.105	[−0.335, +0.126]	−0.196	[−0.472, +0.080]
0.500-00	<b>−1.105</b>	[−1.388, −0.821]	<b>−1.054</b>	[−1.357, −0.752]	<b>−1.040</b>	[−1.290, −0.791]

  

$n^2/1000$ CPU seconds						
	ACS-EE(d) vs. MMAS-EE(d)		ACS-EE(d) vs. RAS-EE(d)		ACS-EE(d) vs. BWAS-EE(d)	
$p$	Difference	95% CI	Difference	95% CI	Difference	95% CI
0.050-00	<b>−0.440</b>	[−0.642, −0.238]	<b>−0.335</b>	[−0.540, −0.131]	−0.036	[−0.241, +0.169]
0.075-00	<b>−0.440</b>	[−0.640, −0.240]	<b>−0.317</b>	[−0.492, −0.142]	−0.133	[−0.337, +0.071]
0.100-00	<b>−0.365</b>	[−0.514, −0.215]	<b>−0.413</b>	[−0.565, −0.260]	−0.133	[−0.327, +0.061]
0.150-00	<b>−0.982</b>	[−1.154, −0.811]	<b>−1.557</b>	[−1.724, −1.391]	<b>−0.629</b>	[−0.773, −0.485]
0.175-00	<b>−0.999</b>	[−1.182, −0.816]	<b>−1.982</b>	[−2.100, −1.863]	<b>−0.563</b>	[−0.749, −0.377]
0.200-00	<b>−1.032</b>	[−1.231, −0.834]	<b>−2.350</b>	[−2.532, −2.168]	<b>−0.667</b>	[−0.853, −0.481]
0.300-00	<b>−0.830</b>	[−1.055, −0.605]	<b>−3.429</b>	[−3.574, −3.284]	<b>−0.515</b>	[−0.710, −0.321]
0.400-00	<b>−0.396</b>	[−0.530, −0.262]	<b>−3.652</b>	[−3.791, −3.513]	<b>−0.479</b>	[−0.605, −0.354]
0.500-00	+0.024	[−0.098, +0.147]	<b>−3.452</b>	[−3.592, −3.311]	<b>−0.276</b>	[−0.429, −0.124]

Table 47: Comparison of the average cost obtained by ACS-EE(d), MMAS-EE(d), RAS-EE(d), and BWAS-EE(d), on the clustered instances of size 1000.

$n^2/10000$ CPU seconds						
	ACS-EE(d) vs. MMAS-EE(d)		ACS-EE(d) vs. RAS-EE(d)		ACS-EE(d) vs. BWAS-EE(d)	
$p$	Difference	95% CI	Difference	95% CI	Difference	95% CI
0.050	+2.669	[+0.613, +4.726]	+1.435	[-0.582, +3.451]	+0.748	[-1.386, +2.883]
0.075	-2.838	[-3.421, -2.255]	-3.417	[-4.030, -2.803]	-3.144	[-3.649, -2.638]
0.100	-3.905	[-4.362, -3.448]	-1.642	[-2.049, -1.235]	-1.057	[-1.729, -0.385]
0.125	-0.983	[-1.180, -0.786]	-0.511	[-0.716, -0.306]	-0.139	[-0.308, +0.029]
0.150	-0.696	[-0.882, -0.511]	-0.605	[-0.838, -0.373]	-0.117	[-0.289, +0.055]
0.175	-1.034	[-1.238, -0.830]	-0.988	[-1.176, -0.801]	-0.417	[-0.623, -0.212]
0.200	-1.162	[-1.357, -0.968]	-1.081	[-1.257, -0.904]	-0.523	[-0.688, -0.358]
0.3	-2.247	[-2.451, -2.043]	-2.015	[-2.164, -1.866]	-1.175	[-1.374, -0.975]
0.4	-3.111	[-3.323, -2.898]	-2.883	[-3.068, -2.699]	-1.586	[-1.773, -1.399]
0.5	-3.319	[-3.528, -3.110]	-3.293	[-3.477, -3.109]	-1.725	[-1.925, -1.525]
0.6	-3.259	[-3.443, -3.075]	-3.572	[-3.764, -3.380]	-1.681	[-1.864, -1.499]

$n^2/1000$ CPU seconds						
	ACS-EE(d) vs. MMAS-EE(d)		ACS-EE(d) vs. RAS-EE(d)		ACS-EE(d) vs. BWAS-EE(d)	
$p$	Difference	95% CI	Difference	95% CI	Difference	95% CI
0.050	-1.893	[-2.222, -1.563]	-1.076	[-1.427, -0.725]	-0.905	[-1.176, -0.635]
0.075	-1.803	[-2.008, -1.599]	-1.371	[-1.517, -1.224]	-0.827	[-1.010, -0.643]
0.100	-0.746	[-0.846, -0.646]	-0.700	[-0.793, -0.608]	-0.378	[-0.464, -0.293]
0.125	-0.653	[-0.716, -0.590]	-0.824	[-0.892, -0.757]	-0.427	[-0.502, -0.352]
0.150	-0.790	[-0.873, -0.708]	-1.262	[-1.363, -1.160]	-0.566	[-0.655, -0.477]
0.175	-0.925	[-1.032, -0.818]	-1.738	[-1.831, -1.644]	-0.553	[-0.637, -0.468]
0.200	-0.956	[-1.057, -0.856]	-2.120	[-2.236, -2.004]	-0.451	[-0.544, -0.358]
0.3	-0.618	[-0.730, -0.506]	-3.189	[-3.307, -3.070]	-0.275	[-0.379, -0.172]
0.4	-0.230	[-0.327, -0.134]	-3.608	[-3.769, -3.447]	-0.292	[-0.402, -0.181]
0.5	-0.139	[-0.246, -0.032]	-3.900	[-4.031, -3.768]	-0.406	[-0.501, -0.310]
0.6	+0.065	[-0.036, +0.167]	-3.881	[-4.056, -3.706]	-0.174	[-0.274, -0.074]

Table 48: Comparison of the average cost obtained by ACS-EE(d), MMAS-EE(d), RAS-EE(d), and BWAS-EE(d), on the uniform instances of size 1000.

$n^2/10000$ CPU seconds						
	ACS-EE(d) vs. MMAS-EE(d)		ACS-EE(d) vs. RAS-EE(d)		ACS-EE(d) vs. BWAS-EE(d)	
$p$	Difference	95% CI	Difference	95% CI	Difference	95% CI
0.050	+1.789	[+0.935, +2.643]	+1.454	[+0.502, +2.406]	+0.852	[−0.046, +1.750]
0.075	<b>−2.474</b>	[−2.797, −2.152]	<b>−2.486</b>	[−2.833, −2.140]	<b>−2.511</b>	[−2.801, −2.221]
0.100	<b>−2.200</b>	[−2.351, −2.049]	<b>−0.934</b>	[−1.101, −0.767]	<b>−0.219</b>	[−0.378, −0.059]
0.125	<b>−0.400</b>	[−0.544, −0.256]	<b>−0.460</b>	[−0.601, −0.318]	+0.119	[−0.049, +0.288]
0.150	<b>−0.781</b>	[−0.957, −0.606]	<b>−0.805</b>	[−0.961, −0.649]	−0.059	[−0.224, +0.106]
0.175	<b>−0.965</b>	[−1.156, −0.774]	<b>−1.089</b>	[−1.267, −0.911]	<b>−0.260</b>	[−0.478, −0.043]
0.200	<b>−1.279</b>	[−1.447, −1.111]	<b>−1.468</b>	[−1.636, −1.299]	<b>−0.516</b>	[−0.694, −0.339]
0.3	<b>−2.865</b>	[−3.021, −2.708]	<b>−2.828</b>	[−2.955, −2.701]	<b>−1.583</b>	[−1.766, −1.399]
0.4	<b>−3.441</b>	[−3.600, −3.282]	<b>−3.369</b>	[−3.513, −3.225]	<b>−1.848</b>	[−2.059, −1.638]
0.5	<b>−3.488</b>	[−3.652, −3.324]	<b>−3.588</b>	[−3.716, −3.461]	<b>−1.802</b>	[−1.974, −1.631]
0.6	<b>−2.954</b>	[−3.129, −2.779]	<b>−3.540</b>	[−3.698, −3.382]	<b>−1.269</b>	[−1.453, −1.084]

$n^2/1000$ CPU seconds						
	ACS-EE(d) vs. MMAS-EE(d)		ACS-EE(d) vs. RAS-EE(d)		ACS-EE(d) vs. BWAS-EE(d)	
$p$	Difference	95% CI	Difference	95% CI	Difference	95% CI
0.050	<b>−1.988</b>	[−2.230, −1.747]	<b>−1.661</b>	[−1.844, −1.477]	<b>−1.099</b>	[−1.287, −0.911]
0.075	<b>−1.374</b>	[−1.472, −1.275]	<b>−1.273</b>	[−1.399, −1.146]	<b>−0.596</b>	[−0.737, −0.455]
0.100	<b>−0.946</b>	[−1.044, −0.847]	<b>−1.104</b>	[−1.184, −1.023]	<b>−0.589</b>	[−0.693, −0.484]
0.125	<b>−0.966</b>	[−1.087, −0.845]	<b>−1.692</b>	[−1.795, −1.589]	<b>−0.639</b>	[−0.763, −0.516]
0.050	<b>−1.988</b>	[−2.230, −1.747]	<b>−1.661</b>	[−1.844, −1.477]	<b>−1.099</b>	[−1.287, −0.911]
0.075	<b>−1.374</b>	[−1.472, −1.275]	<b>−1.273</b>	[−1.399, −1.146]	<b>−0.596</b>	[−0.737, −0.455]
0.100	<b>−0.946</b>	[−1.044, −0.847]	<b>−1.104</b>	[−1.184, −1.023]	<b>−0.589</b>	[−0.693, −0.484]
0.125	<b>−0.966</b>	[−1.087, −0.845]	<b>−1.692</b>	[−1.795, −1.589]	<b>−0.639</b>	[−0.763, −0.516]
0.150	<b>−0.977</b>	[−1.152, −0.802]	<b>−2.230</b>	[−2.330, −2.130]	<b>−0.559</b>	[−0.670, −0.448]
0.175	<b>−0.947</b>	[−1.088, −0.805]	<b>−2.733</b>	[−2.841, −2.625]	<b>−0.507</b>	[−0.605, −0.408]
0.200	<b>−0.808</b>	[−0.916, −0.699]	<b>−3.024</b>	[−3.135, −2.914]	<b>−0.440</b>	[−0.555, −0.326]
0.3	<b>−0.310</b>	[−0.415, −0.204]	<b>−3.973</b>	[−4.258, −3.688]	<b>−0.298</b>	[−0.408, −0.187]
0.4	−0.014	[−0.130, +0.103]	<b>−4.171</b>	[−4.272, −4.069]	<b>−0.331</b>	[−0.456, −0.206]
0.5	+0.181	[+0.084, +0.277]	<b>−3.945</b>	[−4.059, −3.831]	<b>−0.163</b>	[−0.268, −0.059]
0.6	+0.139	[+0.042, +0.236]	<b>−3.880</b>	[−3.984, −3.775]	<b>−0.153</b>	[−0.242, −0.064]

### **3.2 Comparison between the variants with default and tuned parameter values**

Table 49: Comparison of the average cost obtained by the four variants with tuned values to ones with default values on the instance att532.

$n^2/10000$ CPU seconds								
	ACS-EE(t) vs. ACS-EE(d)			MMAS-EE(t) vs. MMAS-EE(d)			RAS-EE(t) vs. RAS-EE(d)	
$p$	Difference	95% CI	Difference	95% CI	Difference	95% CI	Difference	95% CI
0.050-00	+0.433	[−0.046, +0.911]	+0.134	[−0.236, +0.504]	+0.067	[−0.370, +0.504]	−0.044	[−0.436, +0.349]
0.075-00	−0.029	[−0.494, +0.436]	−0.019	[−0.700, +0.661]	+0.064	[−0.212, +0.340]	+0.019	[−0.355, +0.393]
0.100-00	+0.992	[+0.498, +1.487]	+1.147	[+0.671, +1.624]	+1.155	[+0.718, +1.592]	+0.673	[+0.153, +1.193]
0.150-00	+1.228	[+0.508, +1.948]	+0.680	[−0.124, +1.484]	+1.578	[+1.038, +2.118]	+1.671	[+1.057, +2.286]
0.175-00	+0.963	[+0.253, +1.674]	+0.788	[−0.028, +1.604]	+1.423	[+0.940, +1.907]	+1.308	[+0.557, +2.059]
0.200-00	+1.130	[+0.625, +1.635]	+0.951	[+0.382, +1.519]	+1.383	[+0.723, +2.042]	+0.986	[+0.461, +1.511]
0.300-00	<b>−0.578</b>	[−0.954, −0.201]	<b>−0.497</b>	[−0.965, −0.029]	+1.000	[+0.351, +1.649]	+1.190	[+0.574, +1.806]
0.400-00	−0.156	[−0.484, +0.173]	<b>−0.558</b>	[−1.013, −0.104]	+0.205	[−0.274, +0.684]	+1.434	[+0.772, +2.095]
0.500-00	−0.341	[−0.791, +0.110]	<b>−0.870</b>	[−1.463, −0.278]	+0.558	[+0.146, +0.970]	+1.259	[+0.580, +1.938]

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$n^2/1000$ CPU seconds								
	ACS-EE(t) vs. ACS-EE(d)			MMAS-EE(t) vs. MMAS-EE(d)			RAS-EE(t) vs. RAS-EE(d)	
$p$	Difference	95% CI	Difference	95% CI	Difference	95% CI	Difference	95% CI
0.050-00	<b>−0.219</b>	[−0.299, −0.140]	<b>−0.120</b>	[−0.200, −0.039]	<b>−0.121</b>	[−0.212, −0.029]	<b>−0.227</b>	[−0.335, −0.118]
0.075-00	<b>−0.055</b>	[−0.094, −0.017]	−0.052	[−0.114, +0.011]	−0.025	[−0.081, +0.031]	<b>−0.049</b>	[−0.095, −0.004]
0.100-00	−0.031	[−0.068, +0.006]	<b>−0.173</b>	[−0.217, −0.129]	−0.072	[−0.206, +0.062]	<b>−0.066</b>	[−0.102, −0.030]
0.150-00	+0.095	[−0.100, +0.290]	<b>−0.246</b>	[−0.380, −0.112]	<b>−0.637</b>	[−0.754, −0.520]	−0.085	[−0.230, +0.059]
0.175-00	−0.077	[−0.287, +0.133]	<b>−0.268</b>	[−0.393, −0.142]	<b>−0.563</b>	[−0.704, −0.423]	−0.088	[−0.216, +0.039]
0.200-00	+0.083	[−0.266, +0.432]	<b>−0.152</b>	[−0.282, −0.022]	<b>−0.716</b>	[−0.975, −0.456]	+0.043	[−0.174, +0.260]
0.300-00	+0.155	[−0.136, +0.447]	−0.033	[−0.355, +0.289]	<b>−1.572</b>	[−1.770, −1.374]	−0.146	[−0.444, +0.153]
0.400-00	+0.156	[−0.076, +0.389]	+0.175	[−0.031, +0.380]	<b>−1.277</b>	[−1.462, −1.092]	−0.033	[−0.268, +0.202]
0.500-00	+0.021	[−0.150, +0.191]	+0.120	[−0.042, +0.282]	<b>−1.079</b>	[−1.262, −0.896]	+0.060	[−0.100, +0.220]

Table 50: Comparison of the average cost obtained by the four variants with tuned values to ones with default values on the instance att532.

$n^2/10000$ CPU seconds								
	ACS-EE(t) vs. ACS-EE(d)			MMAS-EE(t) vs. MMAS-EE(d)			RAS-EE(t) vs. RAS-EE(d)	
$p$	Difference	95% CI	Difference	95% CI	Difference	95% CI	Difference	95% CI
0.050-00	+0.732	[+0.054, +1.410]	+0.537	[+0.113, +0.962]	+1.551	[+1.034, +2.068]	+1.541	[+0.784, +2.297]
0.075-00	+0.709	[+0.319, +1.100]	+0.185	[−0.039, +0.409]	+0.576	[+0.155, +0.996]	+0.482	[+0.220, +0.744]
0.100-00	+0.766	[+0.405, +1.126]	+0.620	[+0.295, +0.944]	+1.103	[+0.759, +1.447]	+0.937	[+0.654, +1.220]
0.150-00	+1.106	[+0.641, +1.571]	+0.506	[+0.073, +0.940]	+1.125	[+0.643, +1.607]	+1.024	[+0.667, +1.381]
0.175-00	+1.344	[+0.760, +1.929]	+0.228	[−0.161, +0.617]	+1.186	[+0.700, +1.671]	+1.199	[+0.769, +1.630]
0.200-00	+0.663	[+0.125, +1.202]	+0.600	[+0.217, +0.984]	+1.455	[+0.794, +2.117]	+0.703	[+0.243, +1.164]
0.300-00	+0.047	[−0.355, +0.449]	−0.155	[−0.540, +0.229]	+0.894	[+0.394, +1.394]	+1.105	[+0.567, +1.642]
0.400-00	+0.200	[−0.163, +0.564]	−0.124	[−0.662, +0.415]	+0.636	[+0.153, +1.119]	+1.087	[+0.543, +1.632]
0.500-00	−0.033	[−0.490, +0.424]	<b>−0.372</b>	[−0.689, −0.054]	+0.339	[−0.167, +0.846]	+1.099	[+0.474, +1.723]

$n^2/1000$ CPU seconds								
	ACS-EE(t) vs. ACS-EE(d)			MMAS-EE(t) vs. MMAS-EE(d)			RAS-EE(t) vs. RAS-EE(d)	
$p$	Difference	95% CI	Difference	95% CI	Difference	95% CI	Difference	95% CI
0.050-00	<b>−0.093</b>	[−0.132, −0.053]	<b>−0.349</b>	[−0.444, −0.254]	<b>−0.253</b>	[−0.327, −0.180]	−0.035	[−0.073, +0.002]
0.075-00	<b>−0.047</b>	[−0.077, −0.017]	<b>−0.131</b>	[−0.181, −0.081]	<b>−0.149</b>	[−0.188, −0.110]	<b>−0.083</b>	[−0.116, −0.051]
0.100-00	<b>−0.070</b>	[−0.114, −0.026]	<b>−0.253</b>	[−0.298, −0.207]	<b>−0.315</b>	[−0.386, −0.244]	<b>−0.218</b>	[−0.261, −0.174]
0.150-00	+0.007	[−0.068, +0.082]	<b>−0.383</b>	[−0.492, −0.275]	<b>−0.936</b>	[−1.036, −0.837]	<b>−0.120</b>	[−0.200, −0.040]
0.175-00	+0.006	[−0.120, +0.132]	<b>−0.474</b>	[−0.596, −0.352]	<b>−1.174</b>	[−1.283, −1.066]	−0.066	[−0.187, +0.056]
0.200-00	+0.091	[−0.028, +0.210]	<b>−0.419</b>	[−0.536, −0.302]	<b>−1.289</b>	[−1.506, −1.071]	+0.173	[+0.002, +0.344]
0.300-00	−0.130	[−0.260, +0.001]	<b>−0.163</b>	[−0.312, −0.014]	<b>−2.120</b>	[−2.287, −1.953]	−0.044	[−0.198, +0.109]
0.400-00	−0.062	[−0.202, +0.079]	−0.063	[−0.209, +0.083]	<b>−1.968</b>	[−2.100, −1.836]	−0.014	[−0.188, +0.159]
0.500-00	−0.064	[−0.166, +0.039]	−0.000	[−0.086, +0.085]	<b>−1.892</b>	[−2.047, −1.737]	−0.050	[−0.190, +0.089]

Table 51: Comparison of the average cost obtained by the four variants with tuned values to ones with default values on the instance rat783.

$n^2/10000$ CPU seconds								
	ACS-EE(t) vs. ACS-EE(d)			MMAS-EE(t) vs. MMAS-EE(d)			RAS-EE(t) vs. RAS-EE(d)	
$p$	Difference	95% CI	Difference	95% CI	Difference	95% CI	Difference	95% CI
0.050-00	+0.155	[-0.231, +0.541]	-0.089	[-0.452, +0.274]	+0.231	[-0.315, +0.776]	+0.618	[+0.162, +1.075]
0.075-00	-0.114	[-0.423, +0.194]	-0.130	[-0.349, +0.089]	+0.217	[-0.097, +0.530]	+0.090	[−0.288, +0.467]
0.100-00	+0.130	[-0.104, +0.363]	+0.290	[+0.121, +0.458]	+0.801	[+0.527, +1.075]	+0.732	[+0.465, +0.998]
0.150-00	+0.599	[+0.258, +0.940]	+0.575	[+0.385, +0.765]	+0.530	[+0.337, +0.723]	+0.453	[+0.188, +0.718]
0.175-00	+0.770	[+0.424, +1.117]	+0.327	[+0.073, +0.581]	+0.573	[+0.293, +0.853]	+0.547	[+0.280, +0.813]
0.200-00	+0.837	[+0.489, +1.185]	+0.223	[+0.051, +0.395]	+0.828	[+0.532, +1.124]	+0.545	[+0.262, +0.829]
0.300-00	+0.218	[-0.081, +0.518]	+0.041	[-0.164, +0.246]	+0.404	[+0.109, +0.698]	+0.519	[+0.195, +0.842]
0.400-00	-0.102	[-0.358, +0.154]	<b>-0.294</b>	[-0.554, -0.035]	+0.223	[-0.001, +0.447]	+0.387	[+0.069, +0.705]
0.500-00	-0.070	[-0.314, +0.174]	<b>-0.322</b>	[-0.608, -0.035]	+0.293	[+0.021, +0.565]	+0.570	[+0.299, +0.842]

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$n^2/1000$ CPU seconds								
	ACS-EE(t) vs. ACS-EE(d)			MMAS-EE(t) vs. MMAS-EE(d)			RAS-EE(t) vs. RAS-EE(d)	
$p$	Difference	95% CI	Difference	95% CI	Difference	95% CI	Difference	95% CI
0.050-00	<b>-0.270</b>	[-0.482, -0.059]	<b>-0.654</b>	[-0.839, -0.468]	<b>-0.461</b>	[-0.607, -0.314]	-0.193	[−0.388, +0.003]
0.075-00	<b>-0.232</b>	[-0.403, -0.060]	<b>-0.773</b>	[-0.975, -0.572]	<b>-0.561</b>	[-0.689, -0.433]	<b>-0.212</b>	[−0.388, −0.035]
0.100-00	<b>-0.445</b>	[-0.604, -0.287]	<b>-0.761</b>	[-0.928, -0.594]	<b>-0.750</b>	[-0.884, -0.615]	<b>-0.448</b>	[−0.587, −0.308]
0.150-00	<b>-0.172</b>	[-0.308, -0.037]	<b>-1.050</b>	[-1.215, -0.885]	<b>-1.621</b>	[-1.806, -1.436]	<b>-0.722</b>	[−0.898, −0.546]
0.175-00	-0.064	[-0.196, +0.068]	<b>-1.024</b>	[-1.232, -0.816]	<b>-2.170</b>	[-2.339, -2.000]	<b>-0.577</b>	[−0.796, −0.359]
0.200-00	-0.112	[-0.278, +0.054]	<b>-1.090</b>	[-1.256, -0.925]	<b>-2.418</b>	[-2.543, -2.293]	<b>-0.597</b>	[−0.756, −0.437]
0.300-00	+0.255	[+0.104, +0.406]	<b>-0.768</b>	[-0.952, -0.584]	<b>-3.396</b>	[-3.519, -3.273]	<b>-0.216</b>	[−0.396, −0.037]
0.400-00	+0.059	[-0.131, +0.249]	<b>-0.248</b>	[-0.396, -0.101]	<b>-3.280</b>	[-3.446, -3.113]	-0.103	[−0.279, +0.073]
0.500-00	-0.017	[-0.175, +0.141]	-0.007	[-0.164, +0.149]	<b>-3.082</b>	[-3.234, -2.929]	-0.047	[−0.160, +0.067]

Table 52: Comparison of the average cost obtained by the four variants with tuned values to ones with default values on the clustered instances of size 1000.

$n^2/10000$ CPU seconds								
	ACS-EE(t) vs. ACS-EE(d)			MMAS-EE(t) vs. MMAS-EE(d)			RAS-EE(t) vs. RAS-EE(d)	
$p$	Difference	95% CI	Difference	95% CI	Difference	95% CI	Difference	95% CI
0.050	<b>-8.051</b>	[-9.708, -6.394]	<b>-5.030</b>	[-6.240, -3.819]	<b>-8.629</b>	[-10.088, -7.170]	<b>-7.874</b>	[-9.468, -6.281]
0.075	<b>-2.177</b>	[-2.727, -1.626]	<b>-5.838</b>	[-6.372, -5.305]	<b>-6.998</b>	[-7.582, -6.413]	<b>-5.706</b>	[-6.130, -5.282]
0.100	-0.208	[-0.486, +0.070]	<b>-4.813</b>	[-5.248, -4.378]	<b>-2.795</b>	[-3.143, -2.448]	<b>-1.741</b>	[-2.480, -1.001]
0.125	<b>-0.824</b>	[-0.966, -0.683]	<b>-1.832</b>	[-2.022, -1.641]	<b>-1.185</b>	[-1.352, -1.017]	<b>-0.799</b>	[-0.943, -0.655]
0.150	<b>-1.060</b>	[-1.278, -0.842]	<b>-1.751</b>	[-1.924, -1.579]	<b>-1.754</b>	[-1.950, -1.558]	<b>-1.134</b>	[-1.292, -0.977]
0.175	<b>-0.972</b>	[-1.170, -0.774]	<b>-2.062</b>	[-2.238, -1.885]	<b>-2.046</b>	[-2.170, -1.921]	<b>-1.263</b>	[-1.406, -1.119]
0.200	<b>-1.136</b>	[-1.287, -0.986]	<b>-2.268</b>	[-2.467, -2.069]	<b>-2.227</b>	[-2.423, -2.031]	<b>-1.479</b>	[-1.637, -1.321]
0.3	<b>-0.663</b>	[-0.824, -0.501]	<b>-2.779</b>	[-2.968, -2.591]	<b>-2.654</b>	[-2.826, -2.482]	<b>-1.577</b>	[-1.766, -1.388]
0.4	<b>-0.443</b>	[-0.612, -0.274]	<b>-3.282</b>	[-3.486, -3.077]	<b>-3.242</b>	[-3.435, -3.050]	<b>-1.601</b>	[-1.804, -1.399]
0.5	-0.053	[-0.178, +0.071]	<b>-3.192</b>	[-3.393, -2.991]	<b>-3.099</b>	[-3.297, -2.900]	<b>-1.157</b>	[-1.364, -0.949]
0.6	+0.074	[-0.063, +0.210]	<b>-3.146</b>	[-3.333, -2.958]	<b>-2.968</b>	[-3.164, -2.773]	<b>-0.791</b>	[-0.981, -0.601]

$n^2/1000$ CPU seconds								
	ACS-EE(t) vs. ACS-EE(d)			MMAS-EE(t) vs. MMAS-EE(d)			RAS-EE(t) vs. RAS-EE(d)	
$p$	Difference	95% CI	Difference	95% CI	Difference	95% CI	Difference	95% CI
0.050	<b>-1.138</b>	[-1.423, -0.852]	<b>-2.641</b>	[-2.944, -2.338]	<b>-2.819</b>	[-3.062, -2.577]	<b>-1.654</b>	[-1.902, -1.405]
0.075	<b>-0.297</b>	[-0.360, -0.234]	<b>-2.077</b>	[-2.283, -1.871]	<b>-1.670</b>	[-1.812, -1.528]	<b>-1.094</b>	[-1.299, -0.888]
0.100	<b>-0.216</b>	[-0.260, -0.173]	<b>-0.949</b>	[-1.055, -0.843]	<b>-0.918</b>	[-1.016, -0.820]	<b>-0.582</b>	[-0.671, -0.494]
0.125	<b>-0.133</b>	[-0.186, -0.080]	<b>-0.810</b>	[-0.873, -0.747]	<b>-0.983</b>	[-1.052, -0.914]	<b>-0.618</b>	[-0.701, -0.535]
0.150	<b>-0.155</b>	[-0.223, -0.088]	<b>-0.941</b>	[-1.040, -0.842]	<b>-1.436</b>	[-1.532, -1.340]	<b>-0.681</b>	[-0.778, -0.585]
0.175	-0.038	[-0.111, +0.035]	<b>-1.056</b>	[-1.159, -0.954]	<b>-1.834</b>	[-1.921, -1.746]	<b>-0.610</b>	[-0.692, -0.529]
0.200	<b>-0.087</b>	[-0.170, -0.004]	<b>-1.067</b>	[-1.153, -0.980]	<b>-2.134</b>	[-2.257, -2.012]	<b>-0.440</b>	[-0.536, -0.345]
0.3	<b>+0.186</b>	[+0.077, +0.295]	<b>-0.721</b>	[-0.819, -0.624]	<b>-3.188</b>	[-3.294, -3.083]	<b>-0.106</b>	[-0.210, -0.001]
0.4	<b>+0.073</b>	[-0.016, +0.162]	<b>-0.228</b>	[-0.319, -0.138]	<b>-3.393</b>	[-3.570, -3.217]	-0.066	[-0.168, +0.036]
0.5	<b>+0.104</b>	[-0.001, +0.210]	-0.089	[-0.184, +0.007]	<b>-3.531</b>	[-3.663, -3.399]	-0.104	[-0.225, +0.017]
0.6	-0.024	[-0.122, +0.075]	-0.023	[-0.122, +0.076]	<b>-3.475</b>	[-3.645, -3.304]	+0.033	[-0.045, +0.110]

Table 53: Comparison of the average cost obtained by the four variants with tuned values to ones with default values on the uniform instances of size 1000.

$n^2/10000$ CPU seconds												
	ACS-EE(t) vs. ACS-EE(d)			MMAS-EE(t) vs. MMAS-EE(d)			RAS-EE(t) vs. RAS-EE(d)			BWAS-EE(t) vs. BWAS-EE(d)		
$p$	Difference	95% CI	Difference	95% CI	Difference	95% CI	Difference	95% CI	Difference	95% CI		
0.050	<b>-4.932</b>	[-5.876, -3.988]	<b>-3.053</b>	[-3.484, -2.623]	<b>-4.877</b>	[-5.409, -4.344]	<b>-4.446</b>	[-5.017, -3.874]				
0.075	<b>-1.655</b>	[-1.863, -1.446]	<b>-4.507</b>	[-4.774, -4.241]	<b>-4.871</b>	[-5.191, -4.550]	<b>-4.380</b>	[-4.659, -4.102]				
0.100	+0.098	[−0.052, +0.248]	<b>-2.889</b>	[-3.071, -2.708]	<b>-1.755</b>	[-1.960, -1.549]	<b>-0.775</b>	[-0.962, -0.588]				
0.150	<b>-1.093</b>	[-1.269, -0.916]	<b>-1.957</b>	[-2.106, -1.809]	<b>-2.016</b>	[-2.149, -1.882]	<b>-1.093</b>	[-1.248, -0.938]				
0.175	<b>-1.039</b>	[-1.228, -0.851]	<b>-1.996</b>	[-2.172, -1.820]	<b>-2.085</b>	[-2.263, -1.907]	<b>-1.135</b>	[-1.328, -0.942]				
0.200	<b>-0.727</b>	[-0.920, -0.534]	<b>-2.144</b>	[-2.291, -1.997]	<b>-2.322</b>	[-2.485, -2.159]	<b>-0.890</b>	[-1.128, -0.653]				
0.3	<b>-0.401</b>	[-0.584, -0.219]	<b>-3.280</b>	[-3.432, -3.128]	<b>-3.255</b>	[-3.397, -3.113]	<b>-1.571</b>	[-1.793, -1.349]				
0.4	-0.134	[-0.316, +0.048]	<b>-3.489</b>	[-3.640, -3.337]	<b>-3.276</b>	[-3.417, -3.134]	<b>-1.346</b>	[-1.528, -1.165]				
0.5	+0.194	[+0.034, +0.354]	<b>-3.341</b>	[-3.477, -3.205]	<b>-2.884</b>	[-3.038, -2.730]	<b>-0.870</b>	[-1.051, -0.688]				

57

$n^2/1000$ CPU seconds												
	ACS-EE(t) vs. ACS-EE(d)			MMAS-EE(t) vs. MMAS-EE(d)			RAS-EE(t) vs. RAS-EE(d)			BWAS-EE(t) vs. BWAS-EE(d)		
$p$	Difference	95% CI	Difference	95% CI	Difference	95% CI	Difference	95% CI	Difference	95% CI		
0.050	<b>-1.011</b>	[-1.241, -0.782]	<b>-2.859</b>	[-3.121, -2.598]	<b>-2.917</b>	[-3.144, -2.691]	<b>-2.017</b>	[-2.276, -1.758]				
0.075	<b>-0.356</b>	[-0.555, -0.157]	<b>-1.693</b>	[-1.926, -1.459]	<b>-1.633</b>	[-1.842, -1.424]	<b>-1.024</b>	[-1.215, -0.832]				
0.100	<b>-0.247</b>	[-0.453, -0.042]	<b>-1.237</b>	[-1.428, -1.046]	<b>-1.319</b>	[-1.515, -1.122]	<b>-0.957</b>	[-1.161, -0.753]				
0.150	-0.032	[-0.236, +0.171]	<b>-1.103</b>	[-1.289, -0.917]	<b>-2.267</b>	[-2.490, -2.044]	<b>-0.510</b>	[-0.750, -0.270]				
0.175	+0.057	[-0.152, +0.267]	<b>-0.921</b>	[-1.152, -0.690]	<b>-2.615</b>	[-2.844, -2.386]	<b>-0.378</b>	[-0.595, -0.160]				
0.200	+0.095	[-0.118, +0.309]	<b>-0.754</b>	[-1.008, -0.501]	<b>-2.814</b>	[-3.047, -2.582]	<b>-0.256</b>	[-0.494, -0.019]				
0.3	+0.032	[-0.252, +0.316]	<b>-0.392</b>	[-0.644, -0.141]	<b>-3.865</b>	[-4.071, -3.660]	-0.035	[-0.288, +0.219]				
0.4	-0.017	[-0.304, +0.271]	-0.039	[-0.312, +0.235]	<b>-3.760</b>	[-4.023, -3.497]	+0.007	[-0.266, +0.279]				
0.5	-0.069	[-0.373, +0.235]	+0.051	[-0.236, +0.337]	<b>-3.433</b>	[-3.730, -3.136]	+0.105	[-0.186, +0.396]				

### **3.3 Comparison between the variants with tuned parameter values**

Table 54: The average and the standard deviation of the cost obtained by ACS-EE(t), MMAS-EE(t), RAS-EE(t), and BWAS-EE(t), on the TSPLIB instance ch150 for  $n^2/10000$  CPU seconds. The statistics is computed over 30 runs.

		Algorithm	Solution Cost
		mean	s.d.
$p = 0.050$	MMAS-EE(t)	1774	3
	ACS-EE(t)	1775	2
	RAS-EE(t)	1773	2
	BWAS-EE(t)	1774	2
$p = 0.075$	MMAS-EE(t)	2168	2
	ACS-EE(t)	2169	1
	RAS-EE(t)	2168	2
	BWAS-EE(t)	2169	3
$p = 0.100$	MMAS-EE(t)	2493	6
	ACS-EE(t)	2498	8
	RAS-EE(t)	2496	8
	BWAS-EE(t)	2490	5
$p = 0.150$	MMAS-EE(t)	3055	23
	ACS-EE(t)	3061	26
	RAS-EE(t)	3060	28
	BWAS-EE(t)	3066	25
$p = 0.175$	MMAS-EE(t)	3290	31
	ACS-EE(t)	3281	18
	RAS-EE(t)	3293	19
	BWAS-EE(t)	3298	29
$p = 0.200$	MMAS-EE(t)	3498	44
	ACS-EE(t)	3500	29
	RAS-EE(t)	3502	40
	BWAS-EE(t)	3494	34
$p = 0.300$	MMAS-EE(t)	4145	25
	ACS-EE(t)	4157	43
	RAS-EE(t)	4236	53
	BWAS-EE(t)	4204	61
$p = 0.400$	MMAS-EE(t)	4727	35
	ACS-EE(t)	4729	56
	RAS-EE(t)	4815	92
	BWAS-EE(t)	4801	89
$p = 0.500$	MMAS-EE(t)	5217	49
	ACS-EE(t)	5181	74
	RAS-EE(t)	5303	81
	BWAS-EE(t)	5347	102

Table 55: The average and the standard deviation of the cost obtained by ACS-EE(t), MMAS-EE(t), RAS-EE(t), and BWAS-EE(t), on the TSPLIB instance ch150 for  $n^2/1000$  CPU seconds. The statistics is computed over 30 runs.

		Algorithm	Solution Cost
		mean	s.d.
$p = 0.050$	MMAS-EE(t)	1773	1
	ACS-EE(t)	1774	2
	RAS-EE(t)	1773	1
	BWAS-EE(t)	1774	2
$p = 0.075$	MMAS-EE(t)	2166	1
	ACS-EE(t)	2169	2
	RAS-EE(t)	2166	1
	BWAS-EE(t)	2169	2
$p = 0.100$	MMAS-EE(t)	2486	2
	ACS-EE(t)	2496	8
	RAS-EE(t)	2486	2
	BWAS-EE(t)	2494	8
$p = 0.150$	MMAS-EE(t)	3016	1
	ACS-EE(t)	3016	6
	RAS-EE(t)	3015	2
	BWAS-EE(t)	3016	2
$p = 0.175$	MMAS-EE(t)	3241	3
	ACS-EE(t)	3243	5
	RAS-EE(t)	3243	3
	BWAS-EE(t)	3242	3
$p = 0.200$	MMAS-EE(t)	3421	1
	ACS-EE(t)	3422	6
	RAS-EE(t)	3426	8
	BWAS-EE(t)	3423	3
$p = 0.300$	MMAS-EE(t)	4058	6
	ACS-EE(t)	4062	9
	RAS-EE(t)	4063	9
	BWAS-EE(t)	4058	4
$p = 0.400$	MMAS-EE(t)	4578	10
	ACS-EE(t)	4581	13
	RAS-EE(t)	4589	12
	BWAS-EE(t)	4579	9
$p = 0.500$	MMAS-EE(t)	5009	8
	ACS-EE(t)	5009	9
	RAS-EE(t)	5019	15
	BWAS-EE(t)	5010	10

Table 56: The average and the standard deviation of the cost obtained by **ACS-EE(t)**, **MMAS-EE(t)**, **RAS-EE(t)**, and **BWAS-EE(t)**, on the TSPLIB instance d198 for  $n^2/10000$  CPU seconds. The statistics is computed over 30 runs.

		Algorithm	Solution Cost
		mean	s.d.
$p = 0.050$	MMAS-EE(t)	5629	17
	ACS-EE(t)	5632	24
	RAS-EE(t)	5629	21
	BWAS-EE(t)	5634	20
$p = 0.075$	MMAS-EE(t)	6701	25
	ACS-EE(t)	6700	30
	RAS-EE(t)	6698	27
	BWAS-EE(t)	6700	26
$p = 0.100$	MMAS-EE(t)	7502	50
	ACS-EE(t)	7490	46
	RAS-EE(t)	7480	29
	BWAS-EE(t)	7470	28
$p = 0.150$	MMAS-EE(t)	8689	123
	ACS-EE(t)	8700	102
	RAS-EE(t)	8694	120
	BWAS-EE(t)	8700	105
$p = 0.175$	MMAS-EE(t)	9117	103
	ACS-EE(t)	9239	176
	RAS-EE(t)	9181	140
	BWAS-EE(t)	9135	128
$p = 0.200$	MMAS-EE(t)	9599	157
	ACS-EE(t)	9625	205
	RAS-EE(t)	9577	153
	BWAS-EE(t)	9607	192
$p = 0.300$	MMAS-EE(t)	10687	43
	ACS-EE(t)	10707	52
	RAS-EE(t)	10747	66
	BWAS-EE(t)	10917	228
$p = 0.400$	MMAS-EE(t)	11757	49
	ACS-EE(t)	11759	65
	RAS-EE(t)	11834	64
	BWAS-EE(t)	12024	287
$p = 0.500$	MMAS-EE(t)	12710	70
	ACS-EE(t)	12681	77
	RAS-EE(t)	12758	87
	BWAS-EE(t)	12975	257

Table 57: The average and the standard deviation of the cost obtained by **ACS-EE(t)**, **MMAS-EE(t)**, **RAS-EE(t)**, and **BWAS-EE(t)**, on the TSPLIB instance d198 for  $n^2/1000$  CPU seconds. The statistics is computed over 30 runs.

		Algorithm	Solution Cost	
			mean	s.d.
$p = 0.050$	MMAS-EE(t)	5613	1	
	ACS-EE(t)	5628	20	
	RAS-EE(t)	5612	1	
	BWAS-EE(t)	5633	21	
$p = 0.075$	MMAS-EE(t)	6680	3	
	ACS-EE(t)	6697	24	
	RAS-EE(t)	6677	2	
	BWAS-EE(t)	6693	13	
$p = 0.100$	MMAS-EE(t)	7451	7	
	ACS-EE(t)	7497	64	
	RAS-EE(t)	7447	3	
	BWAS-EE(t)	7472	36	
$p = 0.150$	MMAS-EE(t)	8533	2	
	ACS-EE(t)	8532	2	
	RAS-EE(t)	8533	2	
	BWAS-EE(t)	8534	2	
$p = 0.175$	MMAS-EE(t)	8948	3	
	ACS-EE(t)	8947	2	
	RAS-EE(t)	8948	2	
	BWAS-EE(t)	8949	3	
$p = 0.200$	MMAS-EE(t)	9324	3	
	ACS-EE(t)	9325	2	
	RAS-EE(t)	9326	4	
	BWAS-EE(t)	9323	3	
$p = 0.300$	MMAS-EE(t)	10546	5	
	ACS-EE(t)	10547	5	
	RAS-EE(t)	10549	5	
	BWAS-EE(t)	10548	5	
$p = 0.400$	MMAS-EE(t)	11543	5	
	ACS-EE(t)	11547	7	
	RAS-EE(t)	11561	18	
	BWAS-EE(t)	11550	12	
$p = 0.500$	MMAS-EE(t)	12425	5	
	ACS-EE(t)	12427	4	
	RAS-EE(t)	12443	21	
	BWAS-EE(t)	12428	4	

Table 58: The average and the standard deviation of the cost obtained by ACS-EE(t), MMAS-EE(t), RAS-EE(t), and BWAS-EE(t), on the TSPLIB instance lin318 for  $n^2/10000$  CPU seconds. The statistics is computed over 30 runs.

		Algorithm	Solution Cost
		mean	s.d.
$p = 0.050$	MMAS-EE(t)	12756	121
	ACS-EE(t)	12734	135
	RAS-EE(t)	12704	100
	BWAS-EE(t)	12709	74
$p = 0.075$	MMAS-EE(t)	15218	120
	ACS-EE(t)	15216	86
	RAS-EE(t)	15215	78
	BWAS-EE(t)	15213	87
$p = 0.100$	MMAS-EE(t)	17529	207
	ACS-EE(t)	17585	161
	RAS-EE(t)	17528	172
	BWAS-EE(t)	17452	187
$p = 0.150$	MMAS-EE(t)	21319	331
	ACS-EE(t)	21653	266
	RAS-EE(t)	21458	266
	BWAS-EE(t)	21511	334
$p = 0.175$	MMAS-EE(t)	23004	345
	ACS-EE(t)	23236	290
	RAS-EE(t)	23034	259
	BWAS-EE(t)	23079	401
$p = 0.200$	MMAS-EE(t)	24560	224
	ACS-EE(t)	24759	274
	RAS-EE(t)	24606	369
	BWAS-EE(t)	24546	311
$p = 0.300$	MMAS-EE(t)	28998	272
	ACS-EE(t)	28867	232
	RAS-EE(t)	29361	417
	BWAS-EE(t)	29501	416
$p = 0.400$	MMAS-EE(t)	32740	222
	ACS-EE(t)	32376	270
	RAS-EE(t)	32972	333
	BWAS-EE(t)	33357	464
$p = 0.500$	MMAS-EE(t)	35689	324
	ACS-EE(t)	35156	277
	RAS-EE(t)	36080	284
	BWAS-EE(t)	36448	529

Table 59: The average and the standard deviation of the cost obtained by ACS-EE(t), MMAS-EE(t), RAS-EE(t), and BWAS-EE(t), on the TSPLIB instance lin318 for  $n^2/1000$  CPU seconds. The statistics is computed over 30 runs.

		Algorithm	Solution Cost
		mean	s.d.
$p = 0.050$	MMAS-EE(t)	12609	14
	ACS-EE(t)	12592	10
	RAS-EE(t)	12606	15
	BWAS-EE(t)	12596	10
$p = 0.075$	MMAS-EE(t)	15107	7
	ACS-EE(t)	15103	7
	RAS-EE(t)	15105	8
	BWAS-EE(t)	15103	7
$p = 0.100$	MMAS-EE(t)	17224	9
	ACS-EE(t)	17220	7
	RAS-EE(t)	17230	36
	BWAS-EE(t)	17223	8
$p = 0.150$	MMAS-EE(t)	20748	57
	ACS-EE(t)	20763	83
	RAS-EE(t)	20748	56
	BWAS-EE(t)	20747	49
$p = 0.175$	MMAS-EE(t)	22220	62
	ACS-EE(t)	22208	61
	RAS-EE(t)	22242	69
	BWAS-EE(t)	22223	60
$p = 0.200$	MMAS-EE(t)	23542	66
	ACS-EE(t)	23582	141
	RAS-EE(t)	23583	98
	BWAS-EE(t)	23554	83
$p = 0.300$	MMAS-EE(t)	27945	137
	ACS-EE(t)	28038	116
	RAS-EE(t)	27946	154
	BWAS-EE(t)	27911	149
$p = 0.400$	MMAS-EE(t)	31297	155
	ACS-EE(t)	31271	113
	RAS-EE(t)	31321	114
	BWAS-EE(t)	31281	115
$p = 0.500$	MMAS-EE(t)	33922	89
	ACS-EE(t)	33899	83
	RAS-EE(t)	34040	138
	BWAS-EE(t)	33920	108

Table 60: The average and the standard deviation of the cost obtained by ACS-EE(t), MMAS-EE(t), RAS-EE(t), and BWAS-EE(t), on the TSPLIB instance att532 for  $n^2/10000$  CPU seconds. The statistics is computed over 30 runs.

		Algorithm	Solution Cost
		mean	s.d.
$p = 0.050$	MMAS-EE(t)	26014	263
	ACS-EE(t)	26076	326
	RAS-EE(t)	26283	297
	BWAS-EE(t)	26200	457
$p = 0.075$	MMAS-EE(t)	30198	114
	ACS-EE(t)	30362	269
	RAS-EE(t)	30332	295
	BWAS-EE(t)	30284	177
$p = 0.100$	MMAS-EE(t)	34195	249
	ACS-EE(t)	34354	316
	RAS-EE(t)	34348	249
	BWAS-EE(t)	34284	223
$p = 0.150$	MMAS-EE(t)	40838	478
	ACS-EE(t)	41435	419
	RAS-EE(t)	41061	419
	BWAS-EE(t)	40972	343
$p = 0.175$	MMAS-EE(t)	43605	327
	ACS-EE(t)	44515	541
	RAS-EE(t)	44012	471
	BWAS-EE(t)	43962	407
$p = 0.200$	MMAS-EE(t)	46404	314
	ACS-EE(t)	47194	477
	RAS-EE(t)	46784	630
	BWAS-EE(t)	46536	451
$p = 0.300$	MMAS-EE(t)	55566	437
	ACS-EE(t)	56367	380
	RAS-EE(t)	56000	558
	BWAS-EE(t)	56323	788
$p = 0.400$	MMAS-EE(t)	63121	562
	ACS-EE(t)	63917	469
	RAS-EE(t)	63825	683
	BWAS-EE(t)	63897	641
$p = 0.500$	MMAS-EE(t)	69897	335
	ACS-EE(t)	70250	622
	RAS-EE(t)	70395	681
	BWAS-EE(t)	70762	955

Table 61: The average and the standard deviation of the cost obtained by ACS-EE(t), MMAS-EE(t), RAS-EE(t), and BWAS-EE(t), on the TSPLIB instance att532 for  $n^2/1000$  CPU seconds. The statistics is computed over 30 runs.

		Algorithm	Solution Cost
		mean	s.d.
$p = 0.050$	MMAS-EE(t)	25529	12
	ACS-EE(t)	25524	7
	RAS-EE(t)	25533	11
	BWAS-EE(t)	25534	13
$p = 0.075$	MMAS-EE(t)	29983	14
	ACS-EE(t)	29980	15
	RAS-EE(t)	29977	15
	BWAS-EE(t)	29981	16
$p = 0.100$	MMAS-EE(t)	33733	21
	ACS-EE(t)	33724	16
	RAS-EE(t)	33729	27
	BWAS-EE(t)	33721	15
$p = 0.150$	MMAS-EE(t)	39798	59
	ACS-EE(t)	39786	80
	RAS-EE(t)	39788	42
	BWAS-EE(t)	39823	70
$p = 0.175$	MMAS-EE(t)	42355	80
	ACS-EE(t)	42366	96
	RAS-EE(t)	42397	87
	BWAS-EE(t)	42440	127
$p = 0.200$	MMAS-EE(t)	44797	104
	ACS-EE(t)	44810	105
	RAS-EE(t)	44939	200
	BWAS-EE(t)	44933	176
$p = 0.300$	MMAS-EE(t)	53223	126
	ACS-EE(t)	53148	81
	RAS-EE(t)	53260	144
	BWAS-EE(t)	53279	184
$p = 0.400$	MMAS-EE(t)	60108	147
	ACS-EE(t)	60125	178
	RAS-EE(t)	60280	181
	BWAS-EE(t)	60222	181
$p = 0.500$	MMAS-EE(t)	66170	131
	ACS-EE(t)	66202	138
	RAS-EE(t)	66468	201
	BWAS-EE(t)	66282	126

Table 62: The average and the standard deviation of the cost obtained by ACS-EE(t), MMAS-EE(t), RAS-EE(t), and BWAS-EE(t), on the TSPLIB instance rat783 for  $n^2/10000$  CPU seconds. The statistics is computed over 30 runs.

		Algorithm	Solution Cost
		mean	s.d.
$p = 0.050$	MMAS-EE(t)	26014	263
	ACS-EE(t)	26076	326
	RAS-EE(t)	26283	297
	BWAS-EE(t)	26200	457
$p = 0.075$	MMAS-EE(t)	30198	114
	ACS-EE(t)	30362	269
	RAS-EE(t)	30332	295
	BWAS-EE(t)	30284	177
$p = 0.100$	MMAS-EE(t)	34195	249
	ACS-EE(t)	34354	316
	RAS-EE(t)	34348	249
	BWAS-EE(t)	34284	223
$p = 0.150$	MMAS-EE(t)	40838	478
	ACS-EE(t)	41435	419
	RAS-EE(t)	41061	419
	BWAS-EE(t)	40972	343
$p = 0.175$	MMAS-EE(t)	43605	327
	ACS-EE(t)	44515	541
	RAS-EE(t)	44012	471
	BWAS-EE(t)	43962	407
$p = 0.200$	MMAS-EE(t)	46404	314
	ACS-EE(t)	47194	477
	RAS-EE(t)	46784	630
	BWAS-EE(t)	46536	451
$p = 0.300$	MMAS-EE(t)	55566	437
	ACS-EE(t)	56367	380
	RAS-EE(t)	56000	558
	BWAS-EE(t)	56323	788
$p = 0.400$	MMAS-EE(t)	63121	562
	ACS-EE(t)	63917	469
	RAS-EE(t)	63825	683
	BWAS-EE(t)	63897	641
$p = 0.500$	MMAS-EE(t)	69897	335
	ACS-EE(t)	70250	622
	RAS-EE(t)	70395	681
	BWAS-EE(t)	70762	955

Table 63: The average and the standard deviation of the cost obtained by ACS-EE(t), MMAS-EE(t), RAS-EE(t), and BWAS-EE(t), on the TSPLIB instance rat783 for  $n^2/1000$  CPU seconds. The statistics is computed over 30 runs.

		Algorithm	Solution Cost
		mean	s.d.
$p = 0.050$	MMAS-EE(t)	2327	3
	ACS-EE(t)	2325	4
	RAS-EE(t)	2329	5
	BWAS-EE(t)	2331	4
$p = 0.075$	MMAS-EE(t)	2825	5
	ACS-EE(t)	2825	6
	RAS-EE(t)	2826	5
	BWAS-EE(t)	2828	5
$p = 0.100$	MMAS-EE(t)	3250	5
	ACS-EE(t)	3250	4
	RAS-EE(t)	3253	8
	BWAS-EE(t)	3252	5
$p = 0.150$	MMAS-EE(t)	3968	7
	ACS-EE(t)	3964	9
	RAS-EE(t)	3965	9
	BWAS-EE(t)	3968	11
$p = 0.175$	MMAS-EE(t)	4279	10
	ACS-EE(t)	4277	8
	RAS-EE(t)	4274	9
	BWAS-EE(t)	4279	10
$p = 0.200$	MMAS-EE(t)	4560	9
	ACS-EE(t)	4560	10
	RAS-EE(t)	4562	10
	BWAS-EE(t)	4566	10
$p = 0.300$	MMAS-EE(t)	5517	15
	ACS-EE(t)	5527	14
	RAS-EE(t)	5518	11
	BWAS-EE(t)	5528	15
$p = 0.400$	MMAS-EE(t)	6254	15
	ACS-EE(t)	6249	15
	RAS-EE(t)	6270	13
	BWAS-EE(t)	6268	15
$p = 0.500$	MMAS-EE(t)	6868	16
	ACS-EE(t)	6871	16
	RAS-EE(t)	6898	24
	BWAS-EE(t)	6891	16

Table 64: The average and the standard deviation of the cost obtained by ACS-EE(t), MMAS-EE(t), RAS-EE(t), and BWAS-EE(t), on the clustered instances of size 1000 for  $n^2/10000$  CPU seconds. The statistics is computed over 50 instances.

		Algorithm	Solution Cost	
			mean	s.d.
$p = 0.050$	MMAS-EE(t)	4154669	452491	
	ACS-EE(t)	4129846	413981	
	RAS-EE(t)	4045869	408527	
	BWAS-EE(t)	4107063	424843	
$p = 0.075$	MMAS-EE(t)	4479973	418208	
	ACS-EE(t)	4522099	433592	
	RAS-EE(t)	4451324	413349	
	BWAS-EE(t)	4500436	412211	
$p = 0.100$	MMAS-EE(t)	4891716	423719	
	ACS-EE(t)	4928093	422101	
	RAS-EE(t)	4880445	418645	
	BWAS-EE(t)	4904211	420934	
$p = 0.125$	MMAS-EE(t)	5276942	432665	
	ACS-EE(t)	5278680	432332	
	RAS-EE(t)	5286530	433786	
	BWAS-EE(t)	5287407	432039	
$p = 0.150$	MMAS-EE(t)	5636531	441683	
	ACS-EE(t)	5636643	439241	
	RAS-EE(t)	5631215	437036	
	BWAS-EE(t)	5639036	437937	
$p = 0.175$	MMAS-EE(t)	5963852	453152	
	ACS-EE(t)	5967840	448411	
	RAS-EE(t)	5962076	451636	
	BWAS-EE(t)	5975282	446311	
$p = 0.200$	MMAS-EE(t)	6272814	460130	
	ACS-EE(t)	6271695	460155	
	RAS-EE(t)	6270279	455541	
	BWAS-EE(t)	6282823	459022	
$p = 0.300$	MMAS-EE(t)	7354882	498010	
	ACS-EE(t)	7346139	489293	
	RAS-EE(t)	7346943	495163	
	BWAS-EE(t)	7365029	500832	
$p = 0.400$	MMAS-EE(t)	8189628	514667	
	ACS-EE(t)	8167796	520441	
	RAS-EE(t)	8173807	513866	
	BWAS-EE(t)	8202871	523815	
$p = 0.500$	MMAS-EE(t)	8891573	559500	
	ACS-EE(t)	8875149	553337	
	RAS-EE(t)	8897728	549491	
	BWAS-EE(t)	8931251	550048	
$p = 0.600$	MMAS-EE(t)	9489767	572070	
	ACS-EE(t)	9485632	574030	
	RAS-EE(t)	9537968	582504	
	BWAS-EE(t)	9564461	589887	

Table 65: The average and the standard deviation of the cost obtained by ACS-EE(t), MMAS-EE(t), RAS-EE(t), and BWAS-EE(t), on the clustered instances of size 1000 for  $n^2/1000$  CPU seconds. The statistics is computed over 50 instances.

		Algorithm	Solution Cost	
			mean	s.d.
$p = 0.050$	MMAS-EE(t)	3967361	400230	
	ACS-EE(t)	3952366	394118	
	RAS-EE(t)	3927418	389503	
	BWAS-EE(t)	3967641	400511	
$p = 0.075$	MMAS-EE(t)	4427950	402282	
	ACS-EE(t)	4427119	402671	
	RAS-EE(t)	4426817	404066	
	BWAS-EE(t)	4428350	402493	
$p = 0.100$	MMAS-EE(t)	4863055	414240	
	ACS-EE(t)	4862498	415046	
	RAS-EE(t)	4862337	414546	
	BWAS-EE(t)	4863064	414372	
$p = 0.125$	MMAS-EE(t)	5251964	427420	
	ACS-EE(t)	5253255	426528	
	RAS-EE(t)	5251840	426464	
	BWAS-EE(t)	5250149	424944	
$p = 0.150$	MMAS-EE(t)	5603525	436485	
	ACS-EE(t)	5603337	437978	
	RAS-EE(t)	5602156	436425	
	BWAS-EE(t)	5605538	438403	
$p = 0.175$	MMAS-EE(t)	5925723	448196	
	ACS-EE(t)	5931361	448555	
	RAS-EE(t)	5927796	449434	
	BWAS-EE(t)	5930137	447889	
$p = 0.200$	MMAS-EE(t)	6224811	456482	
	ACS-EE(t)	6226358	459295	
	RAS-EE(t)	6230829	457910	
	BWAS-EE(t)	6232441	459464	
$p = 0.300$	MMAS-EE(t)	7245784	489095	
	ACS-EE(t)	7266836	495840	
	RAS-EE(t)	7253354	490057	
	BWAS-EE(t)	7265673	495601	
$p = 0.400$	MMAS-EE(t)	8072748	518515	
	ACS-EE(t)	8078461	522209	
	RAS-EE(t)	8090552	513623	
	BWAS-EE(t)	8090840	518521	
$p = 0.500$	MMAS-EE(t)	8770470	545064	
	ACS-EE(t)	8775206	546671	
	RAS-EE(t)	8799687	540616	
	BWAS-EE(t)	8792614	546606	
$p = 0.600$	MMAS-EE(t)	9373393	567591	
	ACS-EE(t)	9379491	565826	
	RAS-EE(t)	9421367	564999	
	BWAS-EE(t)	9401072	573021	

Table 66: The average and the standard deviation of the cost obtained by ACS-EE(t), MMAS-EE(t), RAS-EE(t), and BWAS-EE(t), on the clustered instances of size 1000 for  $n^2/100$  CPU seconds. The statistics is computed over 50 instances.

		Algorithm	Solution Cost	
			mean	s.d.
$p = 0.050$	MMAS-EE(t)	3918780	420641	
	ACS-EE(t)	3912329	417905	
	RAS-EE(t)	3906280	416594	
	BWAS-EE(t)	3908926	416976	
$p = 0.075$	MMAS-EE(t)	4411445	430096	
	ACS-EE(t)	4410839	430043	
	RAS-EE(t)	4410121	429662	
	BWAS-EE(t)	4410014	430021	
$p = 0.100$	MMAS-EE(t)	4846524	442816	
	ACS-EE(t)	4845178	442968	
	RAS-EE(t)	4847303	443874	
	BWAS-EE(t)	4846073	441653	
$p = 0.125$	MMAS-EE(t)	5235381	454169	
	ACS-EE(t)	5234568	454113	
	RAS-EE(t)	5233427	454719	
	BWAS-EE(t)	5233859	453148	
$p = 0.150$	MMAS-EE(t)	5586270	463489	
	ACS-EE(t)	5584289	464161	
	RAS-EE(t)	5583163	463645	
	BWAS-EE(t)	5587070	465430	
$p = 0.175$	MMAS-EE(t)	5910637	478180	
	ACS-EE(t)	5906468	474885	
	RAS-EE(t)	5906524	471893	
	BWAS-EE(t)	5908820	473720	
$p = 0.200$	MMAS-EE(t)	6206547	483462	
	ACS-EE(t)	6206760	485485	
	RAS-EE(t)	6210050	483186	
	BWAS-EE(t)	6207542	481151	
$p = 0.300$	MMAS-EE(t)	7219962	510793	
	ACS-EE(t)	7220007	511682	
	RAS-EE(t)	7230740	513677	
	BWAS-EE(t)	7226796	514440	
$p = 0.400$	MMAS-EE(t)	8037882	536100	
	ACS-EE(t)	8045408	532753	
	RAS-EE(t)	8072346	529512	
	BWAS-EE(t)	8048145	530967	
$p = 0.500$	MMAS-EE(t)	8736567	553157	
	ACS-EE(t)	8738006	554994	
	RAS-EE(t)	8780395	554992	
	BWAS-EE(t)	8743113	553923	
$p = 0.600$	MMAS-EE(t)	9337342	577163	
	ACS-EE(t)	9346084	584074	
	RAS-EE(t)	9393237	568904	
	BWAS-EE(t)	9349998	572360	

Table 67: The average and the standard deviation of the cost obtained by ACS-EE(t), MMAS-EE(t), RAS-EE(t), and BWAS-EE(t), on the uniform instances of size 1000 for  $n^2/10000$  CPU seconds. The statistics is computed over 50 instances.

		Algorithm	Solution Cost	
			mean	s.d.
$p = 0.050$	MMAS-EE(t)	6699753	84958	
	ACS-EE(t)	6687455	84207	
	RAS-EE(t)	6595473	73064	
	BWAS-EE(t)	6664887	71199	
$p = 0.075$	MMAS-EE(t)	7864904	60155	
	ACS-EE(t)	7899449	68006	
	RAS-EE(t)	7835949	65598	
	BWAS-EE(t)	7878336	63622	
$p = 0.100$	MMAS-EE(t)	8974268	62896	
	ACS-EE(t)	9046815	69103	
	RAS-EE(t)	8963113	79654	
	BWAS-EE(t)	8987604	75374	
$p = 0.125$	MMAS-EE(t)	9936859	65115	
	ACS-EE(t)	9934485	78237	
	RAS-EE(t)	9937183	72885	
	BWAS-EE(t)	9932888	75196	
$p = 0.150$	MMAS-EE(t)	10806490	89448	
	ACS-EE(t)	10816594	83262	
	RAS-EE(t)	10802622	84626	
	BWAS-EE(t)	10822897	81421	
$p = 0.175$	MMAS-EE(t)	11618102	84161	
	ACS-EE(t)	11618340	91368	
	RAS-EE(t)	11622136	106621	
	BWAS-EE(t)	11637411	100128	
$p = 0.200$	MMAS-EE(t)	12353966	88093	
	ACS-EE(t)	12372471	106471	
	RAS-EE(t)	12355056	99701	
	BWAS-EE(t)	12416242	106530	
$p = 0.3$	MMAS-EE(t)	14790544	112933	
	ACS-EE(t)	14794485	110679	
	RAS-EE(t)	14788913	100727	
	BWAS-EE(t)	14855156	106633	
$p = 0.4$	MMAS-EE(t)	16685685	131257	
	ACS-EE(t)	16671647	116385	
	RAS-EE(t)	16710081	118492	
	BWAS-EE(t)	16779312	129706	
$p = 0.5$	MMAS-EE(t)	18251039	166685	
	ACS-EE(t)	18258627	148503	
	RAS-EE(t)	18356361	145789	
	BWAS-EE(t)	18396365	143692	
$p = 0.6$	MMAS-EE(t)	19611667	171425	
	ACS-EE(t)	19601294	184314	
	RAS-EE(t)	19760047	185800	
	BWAS-EE(t)	19766183	184703	

Table 68: The average and the standard deviation of the cost obtained by ACS-EE(t), MMAS-EE(t), RAS-EE(t), and BWAS-EE(t), on the uniform instances of size 1000 for  $n^2/1000$  CPU seconds. The statistics is computed over 50 instances.

		Algorithm	Solution Cost	
			mean	s.d.
$p = 0.050$	MMAS-EE(t)	6491848	52590	
	ACS-EE(t)	6483765	50661	
	RAS-EE(t)	6465669	50237	
	BWAS-EE(t)	6488376	48832	
$p = 0.075$	MMAS-EE(t)	7792539	60274	
	ACS-EE(t)	7789182	57883	
	RAS-EE(t)	7789815	57731	
	BWAS-EE(t)	7784623	58432	
$p = 0.100$	MMAS-EE(t)	8904520	63204	
	ACS-EE(t)	8908003	70583	
	RAS-EE(t)	8910624	64871	
	BWAS-EE(t)	8897612	65940	
$p = 0.125$	MMAS-EE(t)	9868890	69216	
	ACS-EE(t)	9867486	70377	
	RAS-EE(t)	9858016	67898	
	BWAS-EE(t)	9864361	72927	
$p = 0.150$	MMAS-EE(t)	10716389	77806	
	ACS-EE(t)	10726535	79568	
	RAS-EE(t)	10726217	88712	
	BWAS-EE(t)	10735012	80141	
$p = 0.175$	MMAS-EE(t)	11500235	85922	
	ACS-EE(t)	11503696	81004	
	RAS-EE(t)	11510115	89735	
	BWAS-EE(t)	11511693	90725	
$p = 0.200$	MMAS-EE(t)	12209745	88322	
	ACS-EE(t)	12215052	92200	
	RAS-EE(t)	12230311	80961	
	BWAS-EE(t)	12227248	94517	
$p = 0.3$	MMAS-EE(t)	14572689	107869	
	ACS-EE(t)	14588415	114591	
	RAS-EE(t)	14600076	118614	
	BWAS-EE(t)	14622454	113585	
$p = 0.4$	MMAS-EE(t)	16453745	122917	
	ACS-EE(t)	16455445	122368	
	RAS-EE(t)	16529895	131153	
	BWAS-EE(t)	16513191	118816	
$p = 0.5$	MMAS-EE(t)	18021170	135757	
	ACS-EE(t)	18030982	123883	
	RAS-EE(t)	18139365	151093	
	BWAS-EE(t)	18090709	136451	
$p = 0.6$	MMAS-EE(t)	19372737	150802	
	ACS-EE(t)	19382278	157420	
	RAS-EE(t)	19521735	179879	
	BWAS-EE(t)	19420778	180044	

Table 69: The average and the standard deviation of the cost obtained by  $\text{ACS-EE}(t)$ ,  $\text{MMAS-EE}(t)$ ,  $\text{RAS-EE}(t)$ , and  $\text{BWAS-EE}(t)$ , on the uniform instances of size 1000 for  $n^2/100$  CPU seconds. The statistics is computed over 50 instances.

		Algorithm	Solution Cost	
			mean	s.d.
$p = 0.050$		MMAS-EE(t)	6449051	57254
		ACS-EE(t)	6435462	51444
		RAS-EE(t)	6429758	51438
		BWAS-EE(t)	6432187	58952
$p = 0.075$		MMAS-EE(t)	7764054	64957
		ACS-EE(t)	7765313	70626
		RAS-EE(t)	7760715	68723
		BWAS-EE(t)	7760272	72717
$p = 0.100$		MMAS-EE(t)	8884442	73941
		ACS-EE(t)	8888426	83946
		RAS-EE(t)	8895474	90434
		BWAS-EE(t)	8887032	84656
$p = 0.125$		MMAS-EE(t)	9844078	85210
		ACS-EE(t)	9848324	85715
		RAS-EE(t)	9842314	83076
		BWAS-EE(t)	9856090	84739
$p = 0.150$		MMAS-EE(t)	10708924	92816
		ACS-EE(t)	10705984	100268
		RAS-EE(t)	10716376	96932
		BWAS-EE(t)	10705588	100430
$p = 0.175$		MMAS-EE(t)	11475513	105417
		ACS-EE(t)	11497938	103203
		RAS-EE(t)	11502897	100829
		BWAS-EE(t)	11482550	97933
$p = 0.200$		MMAS-EE(t)	12189776	99046
		ACS-EE(t)	12205512	109547
		RAS-EE(t)	12209988	98861
		BWAS-EE(t)	12203464	111042
$p = 0.3$		MMAS-EE(t)	14537333	106584
		ACS-EE(t)	14549235	120152
		RAS-EE(t)	14602640	135624
		BWAS-EE(t)	14572074	116758
$p = 0.4$		MMAS-EE(t)	16403189	144029
		ACS-EE(t)	16441269	148359
		RAS-EE(t)	16506027	121543
		BWAS-EE(t)	16436718	146974
$p = 0.5$		MMAS-EE(t)	17967330	161775
		ACS-EE(t)	17981216	155289
		RAS-EE(t)	18127166	160740
		BWAS-EE(t)	17990635	161565
$p = 0.6$		MMAS-EE(t)	19291402	186547
		ACS-EE(t)	19343449	184152
		RAS-EE(t)	19485059	193581
		BWAS-EE(t)	19326763	190472

Table 70: Comparison of the average cost obtained by ACS-EE(t), MMAS-EE(t), RAS-EE(t), and BWAS-EE(t) over 30 independent runs on instance lin318.

$n^2/10000$ CPU seconds						
	ACS-EE(t) vs. MMAS-EE(t)		ACS-EE(t) vs. RAS-EE(t)		ACS-EE(t) vs. BWAS-EE(t)	
$p$	Difference	95% CI	Difference	95% CI	Difference	95% CI
0.050-00	+0.116	[−0.361, +0.593]	+0.239	[−0.282, +0.759]	+0.299	[−0.247, +0.846]
0.075-00	−0.006	[−0.531, +0.520]	+0.038	[−0.257, +0.333]	+0.088	[−0.196, +0.372]
0.100-00	+0.250	[−0.396, +0.896]	+0.364	[−0.174, +0.902]	+0.664	[+0.089, +1.240]
0.150-00	+1.572	[+0.729, +2.415]	+0.940	[+0.301, +1.579]	+0.734	[+0.009, +1.459]
0.175-00	+0.993	[+0.222, +1.763]	+0.825	[+0.168, +1.482]	+0.556	[−0.249, +1.362]
0.200-00	+0.886	[+0.333, +1.439]	+0.524	[−0.079, +1.127]	+0.756	[+0.139, +1.373]
0.300-00	−0.488	[−0.960, −0.016]	−1.714	[−2.335, −1.093]	−2.068	[−2.654, −1.481]
0.400-00	−1.005	[−1.422, −0.588]	−1.753	[−2.237, −1.269]	−2.890	[−3.517, −2.262]
0.500-00	−1.422	[−1.978, −0.866]	−2.600	[−3.088, −2.112]	−3.344	[−3.941, −2.747]

  

$n^2/1000$ CPU seconds						
	ACS-EE(t) vs. MMAS-EE(t)		ACS-EE(t) vs. RAS-EE(t)		ACS-EE(t) vs. BWAS-EE(t)	
$p$	Difference	95% CI	Difference	95% CI	Difference	95% CI
0.050-00	−0.157	[−0.230, −0.084]	−0.116	[−0.191, −0.041]	−0.022	[−0.076, +0.032]
0.075-00	−0.030	[−0.066, +0.006]	−0.018	[−0.068, +0.033]	+0.002	[−0.038, +0.042]
0.100-00	−0.030	[−0.054, −0.005]	−0.097	[−0.228, +0.033]	−0.016	[−0.052, +0.020]
0.150-00	+0.133	[−0.094, +0.360]	+0.153	[−0.084, +0.390]	+0.110	[−0.085, +0.304]
0.175-00	−0.019	[−0.218, +0.179]	−0.131	[−0.342, +0.080]	−0.028	[−0.195, +0.139]
0.200-00	+0.182	[−0.075, +0.439]	−0.028	[−0.336, +0.279]	+0.128	[−0.124, +0.381]
0.300-00	+0.305	[+0.008, +0.601]	+0.335	[−0.010, +0.679]	+0.392	[+0.113, +0.672]
0.400-00	+0.032	[−0.232, +0.296]	−0.149	[−0.355, +0.057]	+0.012	[−0.241, +0.266]
0.500-00	−0.062	[−0.209, +0.086]	−0.442	[−0.623, −0.261]	−0.075	[−0.233, +0.084]

Table 71: Comparison of the average cost obtained by ACS-EE(t), MMAS-EE(t), RAS-EE(t), and BWAS-EE(t) over 30 independent runs on instance att532.

$n^2/10000$ CPU seconds						
	ACS-EE(t) vs. MMAS-EE(t)		ACS-EE(t) vs. RAS-EE(t)		ACS-EE(t) vs. BWAS-EE(t)	
$p$	Difference	95% CI	Difference	95% CI	Difference	95% CI
0.050-00	+0.286	[−0.323, +0.895]	<b>−0.842</b>	[−1.587, −0.097]	−0.535	[−1.390, +0.320]
0.075-00	+0.558	[+0.079, +1.036]	+0.168	[−0.390, +0.726]	+0.290	[−0.168, +0.748]
0.100-00	+0.564	[+0.094, +1.034]	+0.082	[−0.383, +0.546]	+0.253	[−0.182, +0.688]
0.150-00	+1.544	[+1.005, +2.082]	+0.949	[+0.392, +1.505]	+1.205	[+0.632, +1.778]
0.175-00	+2.188	[+1.658, +2.717]	+1.182	[+0.499, +1.864]	+1.349	[+0.728, +1.971]
0.200-00	+1.629	[+1.241, +2.018]	+0.876	[+0.276, +1.477]	+1.392	[+0.788, +1.996]
0.300-00	+1.479	[+1.135, +1.823]	+0.655	[+0.249, +1.060]	+0.126	[−0.457, +0.709]
0.400-00	+1.238	[+0.809, +1.668]	+0.097	[−0.329, +0.523]	+0.033	[−0.407, +0.473]
0.500-00	+0.445	[+0.000, +0.890]	−0.237	[−0.700, +0.225]	<b>−0.760</b>	[−1.362, −0.158]

  

$n^2/1000$ CPU seconds						
	ACS-EE(t) vs. MMAS-EE(t)		ACS-EE(t) vs. RAS-EE(t)		ACS-EE(t) vs. BWAS-EE(t)	
$p$	Difference	95% CI	Difference	95% CI	Difference	95% CI
0.050-00	−0.021	[−0.048, +0.005]	<b>−0.036</b>	[−0.062, −0.010]	<b>−0.051</b>	[−0.082, −0.020]
0.075-00	+0.000	[−0.041, +0.042]	+0.011	[−0.011, +0.033]	+0.002	[−0.036, +0.039]
0.100-00	−0.026	[−0.061, +0.008]	−0.006	[−0.042, +0.031]	+0.019	[−0.014, +0.051]
0.150-00	−0.031	[−0.135, +0.073]	+0.004	[−0.094, +0.101]	−0.070	[−0.192, +0.052]
0.175-00	+0.023	[−0.102, +0.148]	−0.066	[−0.161, +0.030]	<b>−0.166</b>	[−0.300, −0.032]
0.200-00	+0.018	[−0.122, +0.158]	<b>−0.270</b>	[−0.479, −0.061]	<b>−0.262</b>	[−0.437, −0.087]
0.300-00	−0.118	[−0.253, +0.016]	<b>−0.219</b>	[−0.340, −0.099]	<b>−0.228</b>	[−0.365, −0.092]
0.400-00	+0.029	[−0.085, +0.142]	<b>−0.255</b>	[−0.417, −0.092]	<b>−0.176</b>	[−0.323, −0.029]
0.500-00	+0.064	[−0.051, +0.179]	<b>−0.404</b>	[−0.554, −0.253]	−0.112	[−0.238, +0.013]

Table 72: Comparison of the average cost obtained by ACS-EE(t), MMAS-EE(t), RAS-EE(t), and BWAS-EE(t) over 30 independent runs on instance rat783.

$n^2/10000$ CPU seconds						
	ACS-EE(t) vs. MMAS-EE(t)		ACS-EE(t) vs. RAS-EE(t)		ACS-EE(t) vs. BWAS-EE(t)	
$p$	Difference	95% CI	Difference	95% CI	Difference	95% CI
0.050-00	+0.206	[−0.181, +0.593]	−0.068	[−0.517, +0.381]	<b>−0.565</b>	[−1.093, −0.038]
0.075-00	−0.099	[−0.295, +0.096]	<b>−0.486</b>	[−0.731, −0.241]	<b>−0.343</b>	[−0.618, −0.069]
0.100-00	+0.292	[+0.025, +0.558]	−0.241	[−0.567, +0.084]	−0.088	[−0.431, +0.255]
0.150-00	+1.086	[+0.704, +1.468]	+0.878	[+0.539, +1.217]	+0.879	[+0.524, +1.235]
0.175-00	+1.575	[+1.210, +1.939]	+1.319	[+0.881, +1.758]	+1.239	[+0.877, +1.601]
0.200-00	+1.647	[+1.332, +1.963]	+1.087	[+0.688, +1.485]	+1.325	[+1.006, +1.645]
0.300-00	+0.964	[+0.733, +1.196]	+0.623	[+0.370, +0.875]	+0.315	[+0.006, +0.623]
0.400-00	+0.063	[−0.268, +0.395]	<b>−0.395</b>	[−0.681, −0.110]	<b>−0.691</b>	[−1.002, −0.381]
0.500-00	<b>−0.863</b>	[−1.195, −0.531]	<b>−1.413</b>	[−1.643, −1.184]	<b>−1.665</b>	[−1.926, −1.403]

  

$n^2/1000$ CPU seconds						
	ACS-EE(t) vs. MMAS-EE(t)		ACS-EE(t) vs. RAS-EE(t)		ACS-EE(t) vs. BWAS-EE(t)	
$p$	Difference	95% CI	Difference	95% CI	Difference	95% CI
0.050-00	−0.056	[−0.243, +0.130]	−0.129	[−0.363, +0.105]	−0.205	[−0.440, +0.031]
0.075-00	+0.051	[−0.101, +0.202]	+0.033	[−0.144, +0.210]	−0.071	[−0.221, +0.079]
0.100-00	+0.000	[−0.157, +0.157]	−0.123	[−0.358, +0.112]	−0.109	[−0.272, +0.054]
0.150-00	−0.090	[−0.279, +0.099]	−0.021	[−0.180, +0.139]	−0.079	[−0.246, +0.087]
0.175-00	−0.029	[−0.170, +0.112]	+0.089	[−0.044, +0.221]	−0.050	[−0.209, +0.108]
0.200-00	−0.048	[−0.212, +0.117]	−0.066	[−0.224, +0.093]	−0.175	[−0.363, +0.013]
0.300-00	+0.166	[−0.028, +0.359]	+0.176	[+0.052, +0.300]	−0.033	[−0.181, +0.115]
0.400-00	−0.097	[−0.255, +0.062]	<b>−0.311</b>	[−0.469, −0.154]	<b>−0.306</b>	[−0.451, −0.161]
0.500-00	+0.030	[−0.130, +0.189]	<b>−0.404</b>	[−0.594, −0.214]	<b>−0.247</b>	[−0.400, −0.094]

Table 73: Comparison of the average cost obtained by ACS-EE(t), MMAS-EE(t), RAS-EE(t), and BWAS-EE(t), on the clustered instances of size 1000.

$n^2/10000$ CPU seconds						
	ACS-EE(t) vs. MMAS-EE(t)		ACS-EE(t) vs. RAS-EE(t)		ACS-EE(t) vs. BWAS-EE(t)	
$p$	Difference	95% CI	Difference	95% CI	Difference	95% CI
0.050	-0.597	[-1.498, +0.303]	+2.076	[+1.392, +2.759]	+0.555	[-0.155, +1.264]
0.075	+0.940	[+0.425, +1.455]	+1.590	[+1.184, +1.996]	+0.481	[-0.023, +0.985]
0.100	+0.744	[+0.515, +0.972]	+0.976	[+0.809, +1.143]	+0.487	[+0.297, +0.676]
0.150	+0.002	[-0.156, +0.160]	+0.096	[-0.050, +0.243]	-0.042	[-0.213, +0.128]
0.175	+0.067	[-0.062, +0.196]	+0.097	[-0.025, +0.218]	-0.125	[-0.261, +0.012]
0.200	-0.018	[-0.181, +0.145]	+0.023	[-0.130, +0.175]	-0.177	[-0.307, -0.048]
0.300	-0.119	[-0.262, +0.024]	-0.011	[-0.166, +0.144]	-0.256	[-0.415, -0.098]
0.400	<b>-0.267</b>	[-0.414, -0.119]	-0.074	[-0.229, +0.082]	<b>-0.428</b>	[-0.573, -0.282]
0.500	<b>-0.185</b>	[-0.332, -0.037]	<b>-0.254</b>	[-0.406, -0.102]	<b>-0.628</b>	[-0.757, -0.500]

$n^2/1000$ CPU seconds						
	ACS-EE(t) vs. MMAS-EE(t)		ACS-EE(t) vs. RAS-EE(t)		ACS-EE(t) vs. BWAS-EE(t)	
$p$	Difference	95% CI	Difference	95% CI	Difference	95% CI
0.050	<b>-0.378</b>	[-0.592, -0.164]	+0.635	[+0.445, +0.826]	<b>-0.385</b>	[-0.601, -0.169]
0.075	-0.019	[-0.042, +0.005]	+0.007	[-0.051, +0.064]	<b>-0.028</b>	[-0.055, -0.000]
0.100	-0.011	[-0.045, +0.022]	+0.003	[-0.038, +0.045]	-0.012	[-0.039, +0.016]
0.150	-0.003	[-0.060, +0.053]	+0.021	[-0.037, +0.080]	-0.039	[-0.087, +0.008]
0.175	+0.095	[+0.020, +0.170]	+0.060	[-0.019, +0.140]	+0.021	[-0.051, +0.092]
0.200	+0.025	[-0.046, +0.096]	-0.072	[-0.161, +0.018]	<b>-0.098</b>	[-0.174, -0.021]
0.300	+0.291	[+0.212, +0.369]	+0.186	[+0.106, +0.266]	+0.016	[-0.078, +0.110]
0.400	+0.071	[-0.017, +0.159]	<b>-0.149</b>	[-0.248, -0.051]	<b>-0.153</b>	[-0.234, -0.072]
0.500	+0.054	[-0.047, +0.155]	<b>-0.278</b>	[-0.378, -0.178]	<b>-0.198</b>	[-0.294, -0.102]

Table 74: Comparison of the average cost obtained by ACS-EE, MMAS-EE, RAS-EE, and BWAS-EE, on the clustered instances of size 1000.

$n^2/100$ CPU seconds						
$p$	ACS-EE(t) vs. MMAS-EE(t)			ACS-EE(t) vs. RAS-EE(t)		ACS-EE(t) vs. BWAS-EE(t)
	Difference	95% CI	Difference	95% CI	Difference	95% CI
0.050	<b>-0.165</b>	[-0.258, -0.071]	+0.155	[+0.102, +0.208]	+0.087	[+0.046, +0.128]
0.075	<b>-0.014</b>	[-0.027, -0.000]	+0.016	[-0.002, +0.034]	+0.019	[+0.007, +0.031]
0.100	<b>-0.028</b>	[-0.049, -0.007]	-0.044	[-0.113, +0.025]	-0.018	[-0.044, +0.007]
0.150	-0.035	[-0.078, +0.007]	+0.020	[-0.010, +0.050]	-0.050	[-0.114, +0.015]
0.175	-0.071	[-0.147, +0.006]	-0.001	[-0.072, +0.070]	-0.040	[-0.120, +0.040]
0.200	+0.003	[-0.084, +0.091]	-0.053	[-0.140, +0.034]	-0.013	[-0.121, +0.096]
0.300	+0.001	[-0.068, +0.070]	<b>-0.148</b>	[-0.239, -0.058]	<b>-0.094</b>	[-0.170, -0.018]
0.400	<b>+0.094</b>	[+0.012, +0.175]	<b>-0.334</b>	[-0.471, -0.197]	-0.034	[-0.127, +0.059]
0.500	+0.016	[-0.086, +0.119]	<b>-0.483</b>	[-0.618, -0.348]	-0.058	[-0.135, +0.018]

Table 75: Comparison of the average cost obtained by ACS-EE(t), MMAS-EE(t), RAS-EE(t), and BWAS-EE(t) over 50 uniform instances of size 1000.

$n^2/10000$ CPU seconds						
	ACS-EE(t) vs. MMAS-EE(t)		ACS-EE(t) vs. RAS-EE(t)		ACS-EE(t) vs. BWAS-EE(t)	
$p$	Difference	95% CI	Difference	95% CI	Difference	95% CI
0.050	-0.184	[-0.676, +0.308]	+1.395	[+0.990, +1.799]	+0.339	[-0.028, +0.705]
0.075	+0.439	[+0.279, +0.599]	+0.810	[+0.663, +0.958]	+0.268	[+0.118, +0.417]
0.100	+0.808	[+0.661, +0.955]	+0.934	[+0.738, +1.130]	+0.659	[+0.502, +0.815]
0.150	+0.094	[-0.063, +0.250]	+0.129	[-0.041, +0.300]	-0.058	[-0.244, +0.128]
0.175	+0.002	[-0.185, +0.189]	-0.033	[-0.196, +0.131]	-0.164	[-0.353, +0.025]
0.200	+0.150	[-0.017, +0.317]	+0.141	[-0.063, +0.345]	-0.353	[-0.596, -0.109]
0.300	+0.027	[-0.148, +0.201]	+0.038	[-0.114, +0.190]	-0.414	[-0.639, -0.189]
0.400	-0.084	[-0.255, +0.087]	<b>-0.230</b>	[-0.406, -0.054]	<b>-0.642</b>	[-0.814, -0.469]
0.500	+0.042	[-0.129, +0.212]	<b>-0.532</b>	[-0.697, -0.368]	<b>-0.749</b>	[-0.917, -0.581]

  

$n^2/1000$ CPU seconds						
	ACS-EE(t) vs. MMAS-EE(t)		ACS-EE(t) vs. RAS-EE(t)		ACS-EE(t) vs. BWAS-EE(t)	
$p$	Difference	95% CI	Difference	95% CI	Difference	95% CI
0.050	-0.125	[-0.287, +0.038]	+0.280	[+0.112, +0.448]	-0.071	[-0.283, +0.141]
0.075	-0.043	[-0.133, +0.047]	-0.008	[-0.099, +0.083]	+0.059	[+0.001, +0.116]
0.100	+0.039	[-0.032, +0.110]	-0.029	[-0.148, +0.090]	+0.117	[+0.026, +0.207]
0.150	+0.095	[-0.013, +0.203]	+0.003	[-0.116, +0.122]	-0.079	[-0.197, +0.039]
0.175	+0.030	[-0.054, +0.114]	-0.056	[-0.188, +0.076]	-0.069	[-0.192, +0.053]
0.200	+0.043	[-0.089, +0.176]	<b>-0.125</b>	[-0.242, -0.007]	-0.100	[-0.220, +0.020]
0.300	+0.108	[-0.015, +0.230]	-0.080	[-0.218, +0.058]	<b>-0.233</b>	[-0.340, -0.125]
0.400	+0.010	[-0.108, +0.129]	<b>-0.450</b>	[-0.576, -0.324]	<b>-0.350</b>	[-0.463, -0.237]
0.500	+0.054	[-0.057, +0.166]	<b>-0.598</b>	[-0.738, -0.457]	<b>-0.330</b>	[-0.463, -0.197]

  

$n^2/100$ CPU seconds						
	ACS-EE(t) vs. MMAS-EE(t)		ACS-EE(t) vs. RAS-EE(t)		ACS-EE(t) vs. BWAS-EE(t)	
$p$	Difference	95% CI	Difference	95% CI	Difference	95% CI
0.050	<b>-0.211</b>	[-0.342, -0.080]	+0.089	[-0.007, +0.184]	+0.051	[-0.078, +0.180]
0.075	+0.016	[-0.075, +0.107]	+0.059	[-0.054, +0.172]	+0.065	[-0.027, +0.157]
0.100	+0.045	[-0.101, +0.190]	-0.079	[-0.275, +0.116]	+0.016	[-0.163, +0.194]
0.150	-0.027	[-0.244, +0.189]	-0.097	[-0.233, +0.039]	+0.004	[-0.149, +0.156]
0.175	+0.195	[+0.064, +0.327]	-0.043	[-0.224, +0.138]	+0.134	[-0.012, +0.280]
0.200	+0.129	[-0.066, +0.324]	-0.037	[-0.246, +0.173]	+0.017	[-0.173, +0.207]
0.300	+0.082	[-0.084, +0.248]	<b>-0.366</b>	[-0.572, -0.159]	<b>-0.157</b>	[-0.305, -0.008]
0.400	+0.232	[+0.096, +0.368]	<b>-0.392</b>	[-0.588, -0.197]	+0.028	[-0.120, +0.176]
0.500	+0.077	[-0.089, +0.244]	<b>-0.805</b>	[-1.010, -0.601]	-0.052	[-0.197, +0.092]